NOTE: Because CUDA C is an extension of the C programming language, all of the exercises below must be written in C.

1. Vector Addition Using CUDA C kernel
Here we will write a code that is the “Hello World” equivalent for CUDA C programming, a code that adds two vectors \( A \) and \( B \) of length \( N \), to obtain a third vector \( C = A + B \), element by element.

(a) First write a serial C program that defines three \texttt{float} arrays \( A \), \( B \), and \( C \) of size \( N \). Fill arrays \( A \) and \( B \) with some non-trivial initial values. Then call a function, passing in the vectors \( A \) and \( B \), that computes \( C = A + B \) element by element.

(b) Choose \( N \) large enough that this operation takes a minimum time \( T \) of 10 seconds, but not more than 60 seconds. Due to memory size limitations, you may need to add an outer loop to the code to repeat the calculation \( n \) times, choosing an appropriate value of \( n \) to obtain \( 10 \text{ s} \leq T \leq 60 \text{ s} \). Measure the time it takes to perform this function using the UNIX \texttt{time} command,

\[
\text{time vecadd_serial.e}
\]

(c) Create a CUDA C version of the code (saving the serial C version) that employs a CUDA C kernel to perform the vector addition on the GPU device. Don’t forget to allocate memory on the device for \( A \), \( B \), and \( C \), copy data from host to device and back as necessary, and free the device memory allocation when you are done.

(d) Time the execution of the GPU code using the UNIX \texttt{time} command, as above. Consider whether or not you want the memory allocation and free calls on the device to fall within the outer \( n \) loop. Try it both ways to see if including the memory allocation calls leads to a noticeably longer execution time.

2. Monte Carlo Determination of the Value of \( \pi \) Using the GPU
Here we will use the GPU to compute the value of \( \pi \) using the Monte Carlo method.

(a) Start with the serial C version of the Monte Carlo \( \pi \) code that you wrote for the MPI Programming Exercises. If you wrote that code in Fortran, you will have to translate it to C for this exercise.

(b) If you have not written the serial C version in this manner, modify it so that the value of \( \pi \) is computed in a function call, with the only arguments passed being the number of Monte Carlo points \( N \) and the computed value of \( \pi \) (should by type \texttt{double}).

(c) Time the execution of the code using the UNIX \texttt{time} command, as above, with the likely need to repeat the calculation \( n \) times in an outer loop to obtain \( 10 \text{ s} \leq T \leq 60 \text{ s} \).

(d) Create a CUDA C version of the code (saving the serial C version) that employs a CUDA C kernel to compute the value of \( \pi \) using the Monte Carlo method. Note that generating random numbers on the GPU device (in the CUDA C kernel) is a challenging task. Also note that only \texttt{__device__} functions can be called from within the kernel, so the usual intrinsic random number generator functions in C (which are \texttt{__host__} functions) cannot be used to generate random numbers. You will need to define your own \texttt{__device__} function that generates random numbers—you can use the \texttt{MersenneTwister} CUDA C code from the NVIDIA GPU Computing SDK as a blueprint for writing this \texttt{__device__} function to generate random numbers.

(e) Time the execution of the GPU accelerated code using the UNIX \texttt{time} command, as above.