

A Simple Analytical Model

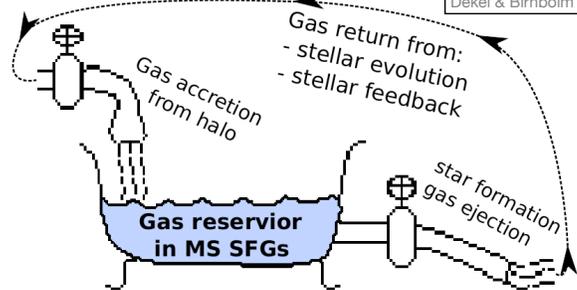
(1) a continuity equation:

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt}$$

Change in Cold Gas Reservoir Accretion Rate \propto Halo Growth Rate Gas Consumption Rate \propto Star Formation Rate

The "Bathtub" Model

Bouche+2010
see also Lilly+2013
Cattaneo+2006
Dekel & Birnboim 2006



A Simple Analytical Model

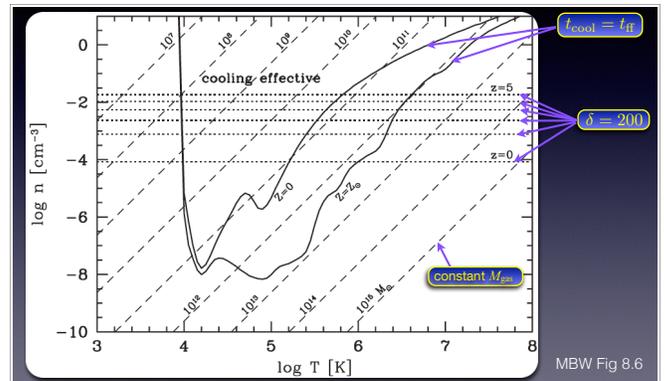
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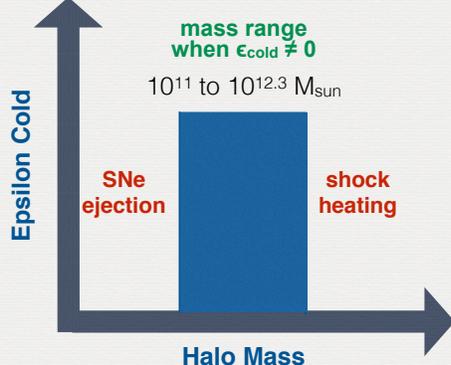
Where stellar growth decouples from halo growth is specified by the cold gas accretion efficiency (ϵ_{cold})

Virialized gas in massive halos cannot cool effectively ($t_{\text{cool}} > t_{\text{ff}}$)



The Cold Gas Accretion Rate

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt}$$



The "Bathtub" Model

First, a continuity equation:

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt}$$

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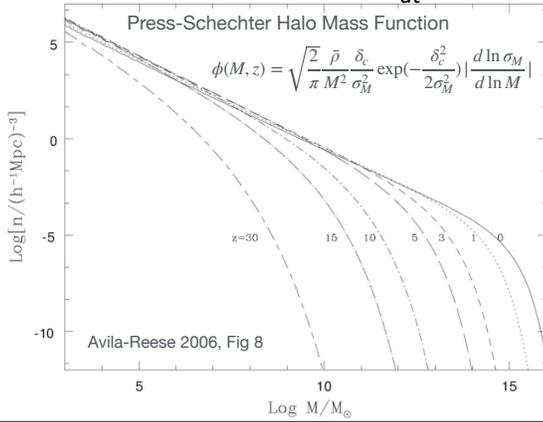
Where stellar growth decouples from halo growth is specified by the cold gas accretion efficiency (ϵ_{cold})

$$\begin{cases} \epsilon_{\text{cold}} = 0.0 & \text{if } M_{\text{halo}} < 10^{11} M_{\odot} \\ \epsilon_{\text{cold}} = 0.7 & \text{if } 10^{11} < M_{\text{halo}} < 10^{12.3} M_{\odot} \\ \epsilon_{\text{cold}} = 0.0 & \text{if } M_{\text{halo}} > 10^{12.3} M_{\odot} \end{cases}$$

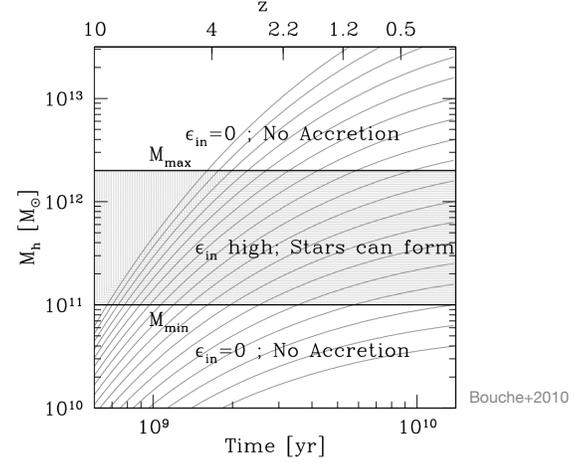
But we need two additional equations to solve the continuity equation.

The "Bathtub" Model

(2) halo growth from extended PS formalism: $\frac{dM_{\text{halo}}}{dt} \propto M_{\text{halo}}^{1.1} (1+z)^{2.2}$

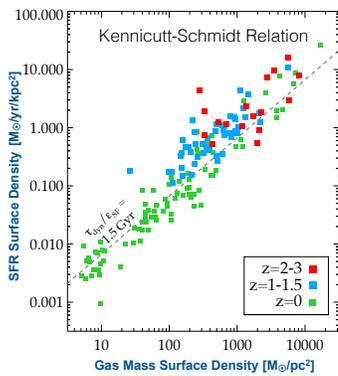


Halo mass vs. redshift & time



The "Bathtub" Model

(3) an equation that relates gas mass and star formation:



$$\frac{dM_{\text{star}}}{dt} = \text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}}$$

$$\text{SFR} \approx M_{\text{gas}} / 10^9 \text{ yr}$$

The "Bathtub" Model: Accretion-Driven Star Formation

a continuity equation coupled with a halo growth history and a star formation law

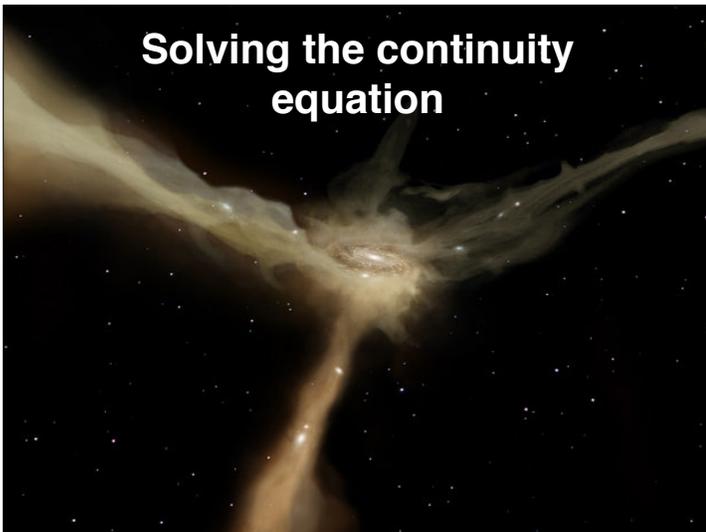
Change in Cold Gas Reservoir \propto Accretion Rate \propto Halo Growth Rate \propto Gas Consumption Rate \propto Star Formation Rate

$$\left\{ \begin{array}{l} \frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt} \\ \frac{dM_{\text{halo}}}{dt} \propto M_{\text{halo}}^{1.1} (1+z)^{2.2} \leftarrow \text{Halo Growth Rate from EPS} \\ \frac{dM_{\text{star}}}{dt} = \text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}} \leftarrow \text{Kennicutt-Schmidt Relation} \end{array} \right.$$

cold gas accretion efficiency: $\epsilon_{\text{cold}} = 0.0$ if $M_{\text{halo}} < 10^{11} M_{\odot}$
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 $\epsilon_{\text{cold}} = 0.0$ if $M_{\text{halo}} > 10^{12.3} M_{\odot}$

recycle & feedback: $f_{\text{recycle}} = 0.5$
 $f_{\text{outflow}} = 0.6$

Solving the continuity equation



The "Bathtub" Model: Accretion-Driven Star Formation

a continuity equation coupled with a halo growth history and a star formation law

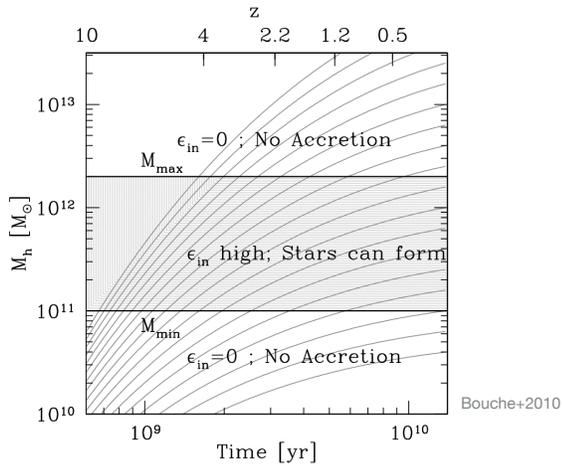
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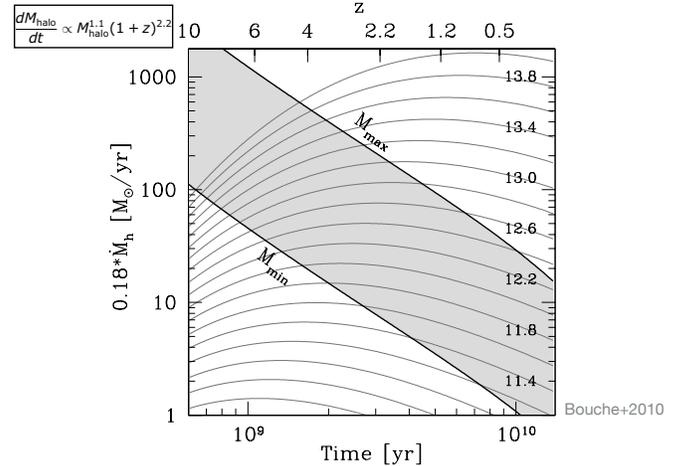
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recycle & feedback: $f_{\text{recycle}} = 0.5$
 $f_{\text{outflow}} = 0.6$

Halo mass vs. redshift & time



Halo growth rate vs. redshift & time



When reservoir stays constant: steady state

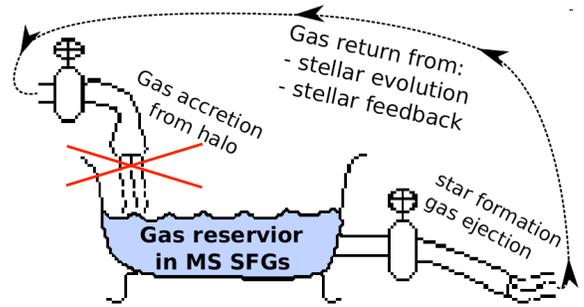
- SFR ~ Accretion Rate
- Gas reservoir filled to SFR x 1 Gyr

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \text{SFR}$$

when $\frac{dM_{\text{gas}}}{dt} = 0$ we have :

$$\text{SFR} = \frac{\epsilon_{\text{cold}} f_{\text{baryon}}}{1 - f_{\text{recycle}} + f_{\text{outflow}}} \frac{dM_{\text{halo}}}{dt} \approx f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} \quad (\text{note the approximation})$$

When cold gas accretion stops: drain the tub



When cold gas accretion stops: drain the tub

SFR exponentially declines with an e-folding time of 2 Gyr

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \text{SFR}$$

$$\text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}} \quad \leftarrow \text{Star Formation Law}$$

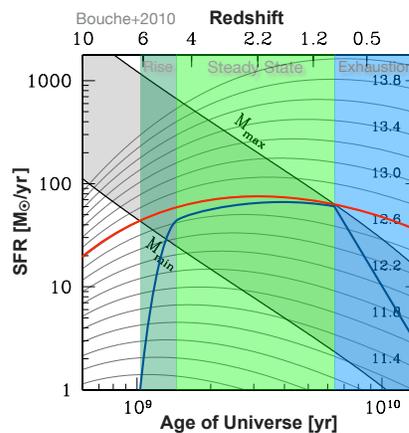
when $\epsilon_{\text{cold}} = 0$ we have :

$$\frac{d\text{SFR}}{dt} = -\frac{\epsilon_{\text{SF}} (1 - f_{\text{recycle}} + f_{\text{outflow}})}{\tau_{\text{dyn}}} \text{SFR}$$

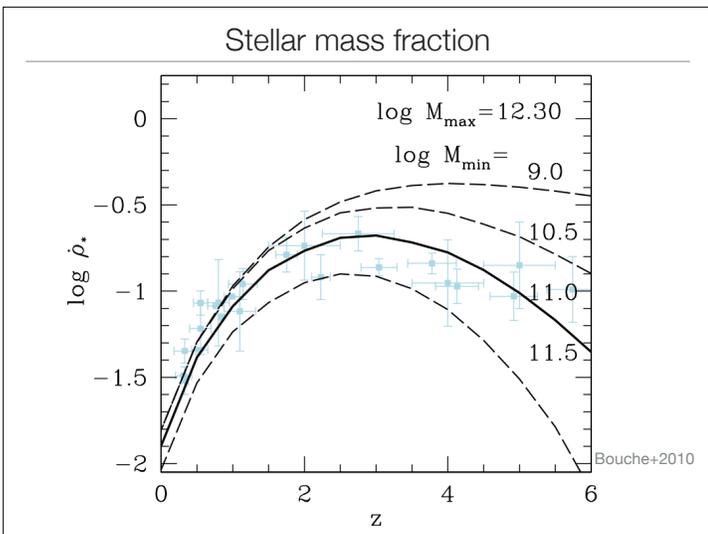
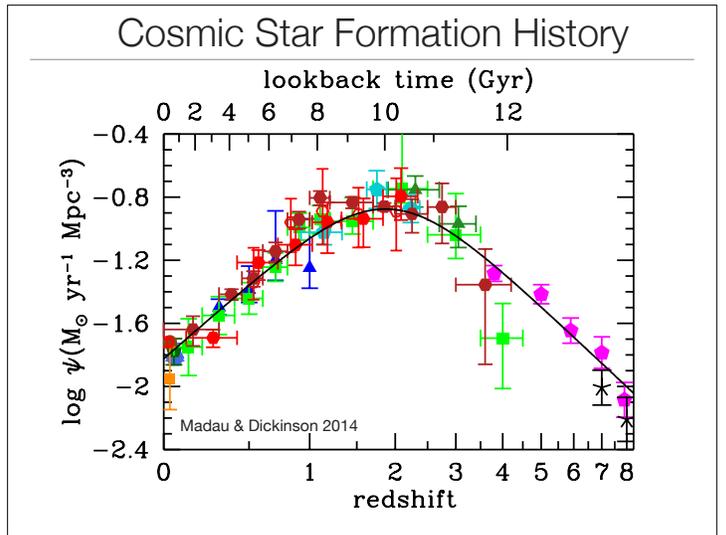
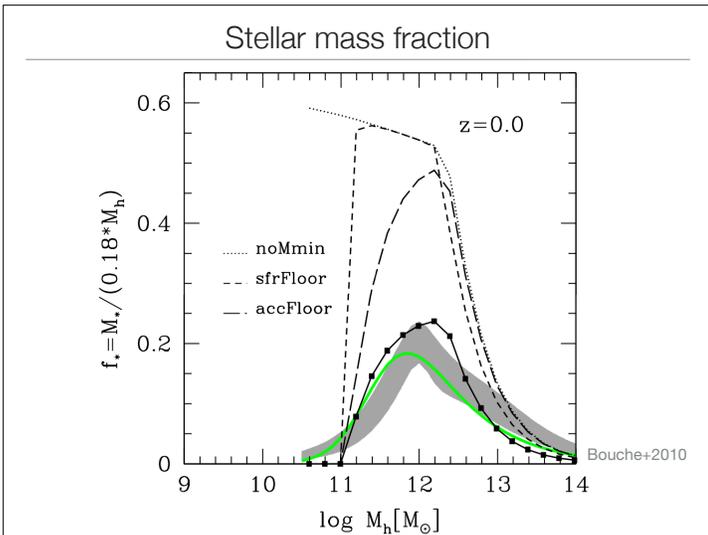
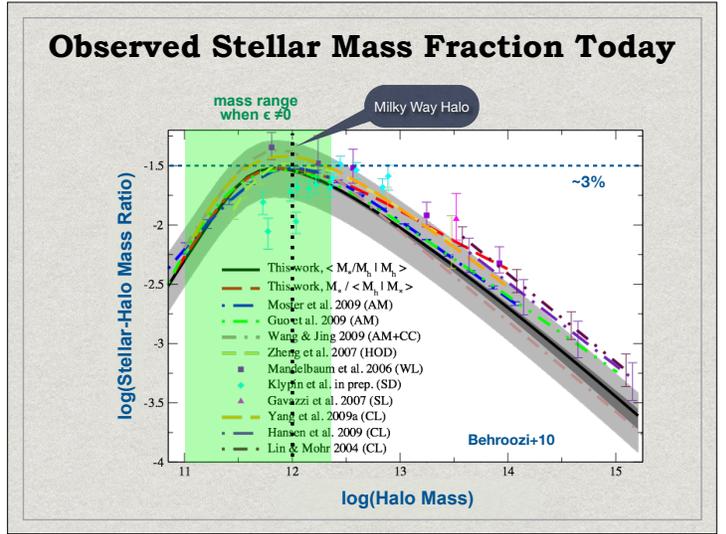
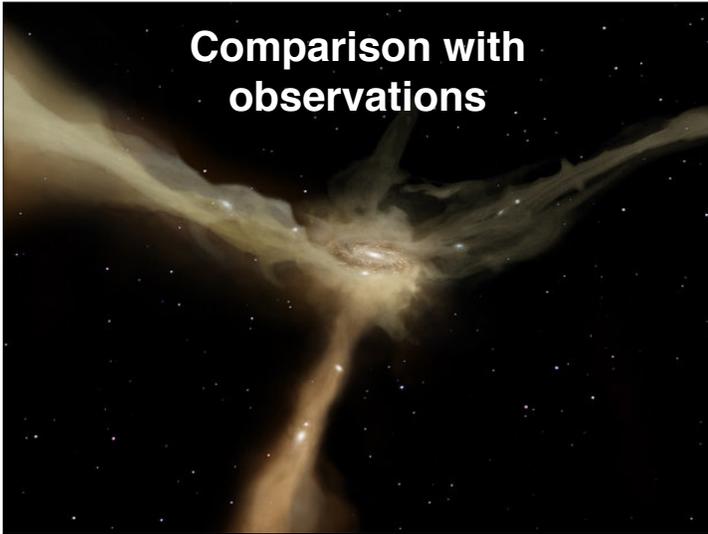
Solving this equation, we get an exponentially declining SFR :

$$\text{SFR} \propto \exp\left(-\frac{t}{\tau}\right) \text{ and } \tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SF}} (1 - f_{\text{recycle}} + f_{\text{outflow}})} \approx 2 \text{ Gyr}$$

Accretion-Driven Star Formation History

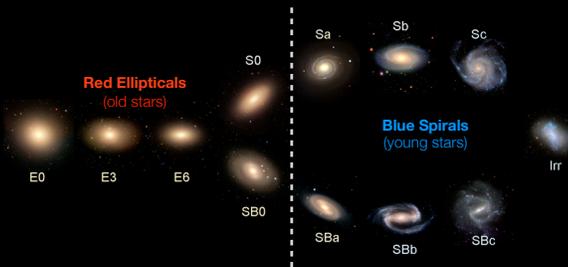


- **Grey region:** efficient cold gas accretion $10^{11} < M_{\text{halo}} < 1.5 \times 10^{12} M_{\odot}$
- **Gas accretion history** of a $10^{12.6} M_{\odot}$ halo (mass at $z = 0$)
- **Star formation history** from the continuity equation:
 1. Once the halo crosses the minimum mass ($10^{11} M_{\odot}$), the SFR rapidly rises to reach a steady state;
 2. As the halo mass reaches $10^{12.3} M_{\odot}$, cold gas accretion is choked and the SFR starts to decline with an e-folding time of 2-3 Gyr ($= 2 \tau_{\text{dyn}} / \epsilon_{\text{SF}}$).



Color Bimodality: Galaxies are either blue or red

Hubble's Galaxy Classification Scheme

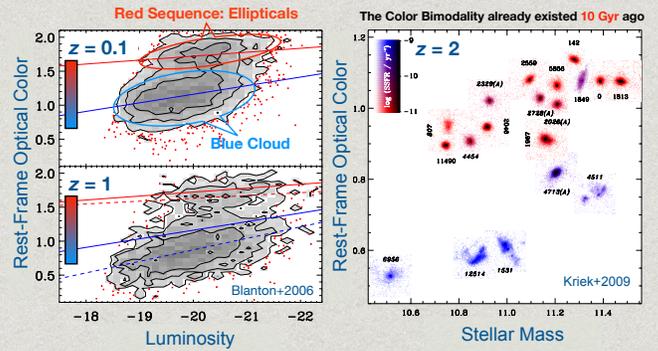


Galaxies in the Current universe

Hai Fu, UC Irvine

Alabama, Apr 17 2013

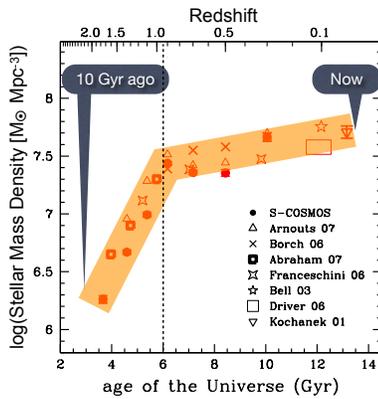
Color Bimodality



The early & rapid build-up of the red sequence

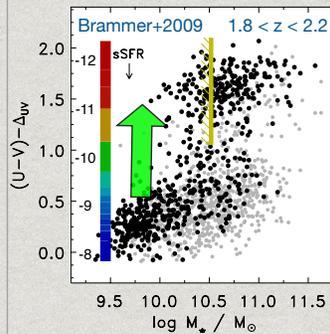
the evolution of the total comoving stellar mass density of quiescent galaxies

- Early Completion:** Most of the stellar mass in the red sequence is already in place by $z = 1$
- Rapid Build-Up:** Stellar mass density increased more than 20x in just 2.5 Gyr ($1 < z < 2$).



Ilbert+2010

Color bimodality at high-redshift requires rapid quenching



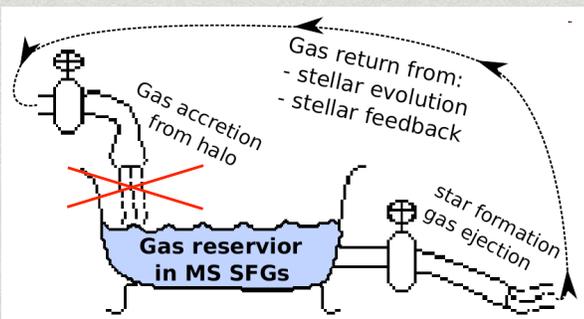
The lack of galaxies between blue cloud and red sequence requires very rapid transition:

- * It takes ~5 e-folding time to cross the green valley ($e^5 = 150$)
- * red-sequence e-folding timescale of 1 Gyr indicates an SFR e-folding time **<0.2 Gyr** (consistent w/ Goncalves+2012)
- This is **10x** shorter than the gas exhaustion time (**~2 Gyr**)!

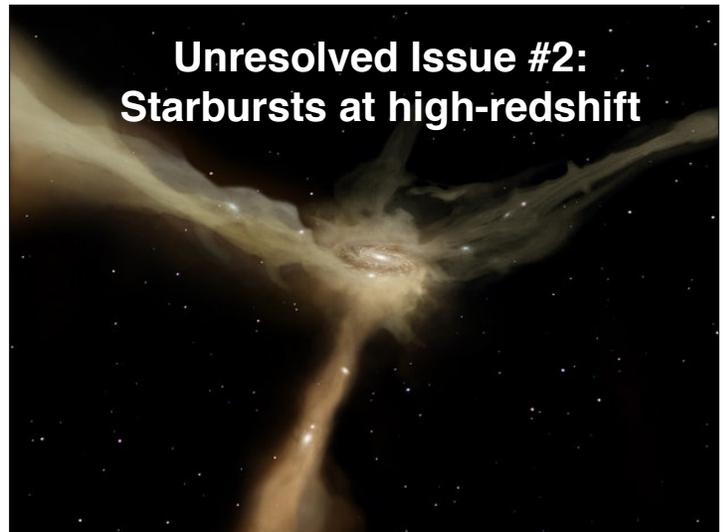
$$\tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SFR}}(1 - f_{\text{recycle}} + f_{\text{outflow}})}$$

How to quench star formation? (i.e. reduce the e-folding time by 10x)

$$\text{SFR} \propto \exp\left(-\frac{t}{\tau}\right) \text{ and } \tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SFR}}(1 - f_{\text{recycle}} + f_{\text{outflow}})} \approx 2 \text{ Gyr}$$

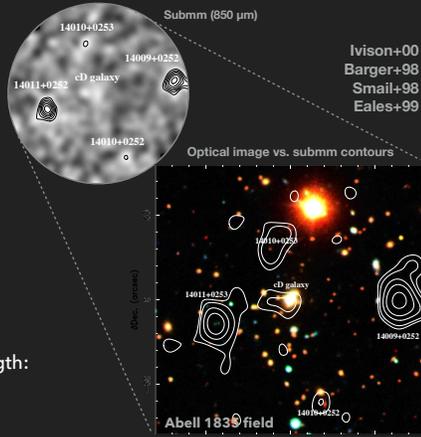


Unresolved Issue #2: Starbursts at high-redshift

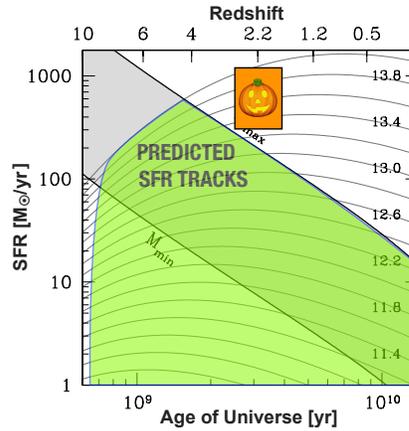


Submm-Bright Galaxies (SMGs) at $z \sim 2.5$

- ▶ SMG definition:
 $S(850\mu\text{m}) > 2\text{-}3\text{ mJy}$
- ▶ Bright in submm, but extremely faint in optical
- ▶ Median properties:
 $\langle z \rangle \sim 2.5$
 $\langle L_{\text{IR}} \rangle \sim 5 \times 10^{12} L_{\odot}$
 $\langle \text{SFR} \rangle \sim 500 M_{\odot}/\text{yr}$
- ▶ Strong clustering strength:
 $M_{\text{halo}} \sim 10^{13} M_{\odot}$
similar to $z \sim 2$ QSOs



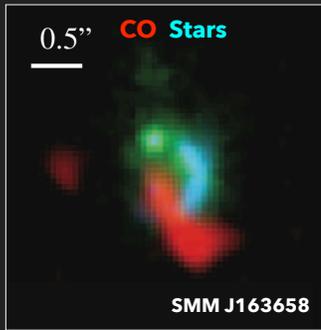
Intense Starburst Galaxies at $z \sim 2$



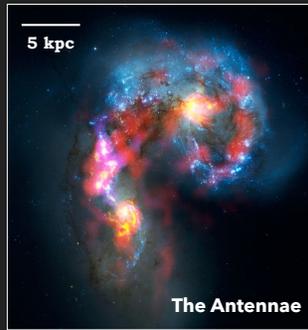
- ▶ **Green region:** star formation tracks of all halos less than $10^{14} M_{\odot}$ at $z = 0$.
- ▶ **Orange:** The SFRs of these galaxies appear too high for any halos at their epoch.

Misaligned stellar and ISM emission

typical offsets: a few kpc ($0.5'' = 4\text{ kpc}$ @ $z = 2.5$)



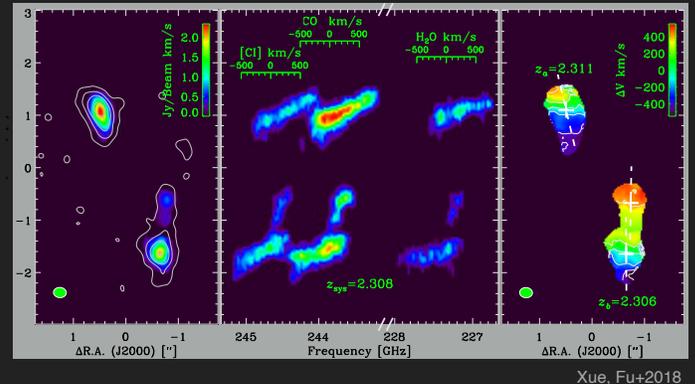
Tacconi+2008



Calistro Rivera+2018

Resolved gas kinematics in an SMG merger

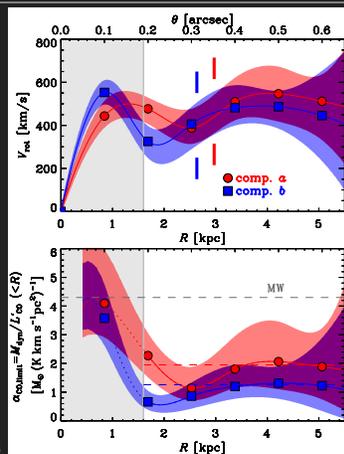
ALMA Cycle 3, 2.6 hr on-source, $0.2''$ spatial resolution, 240 GHz (band 6, $z = 2.308$)
CO J=7-6 @ 806.7 GHz, [C I] $^3\text{P}_2 - ^3\text{P}_1$ @ 809.3 GHz, H₂O 2₁₁ - 2₀₂ @ 752.0 GHz



Xue, Fu+2018

Dynamical mass estimates

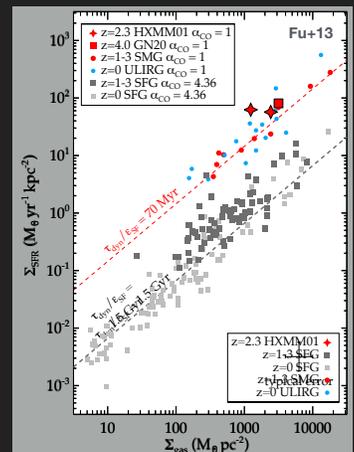
- ▶ Rotation velocities reach 500 km/s (inclination corrected), with a dispersion ~ 160 km/s
- ▶ Dynamical masses:
 $M_{\text{dyn}} \sim 2 \times 10^{11} M_{\text{sun}}$ within 5 kpc
- ▶ CO(1-0) luminosity:
 $L'_{\text{CO}} \sim 1.5 \times 10^{11} K\text{ km/s pc}^2$
- ▶ Upper limits on the CO-to-H₂ conversion factor:
 $M_{\text{H}_2}/L'_{\text{CO}} < 1.5$, much lower than the Galactic GMC value of 4.3.



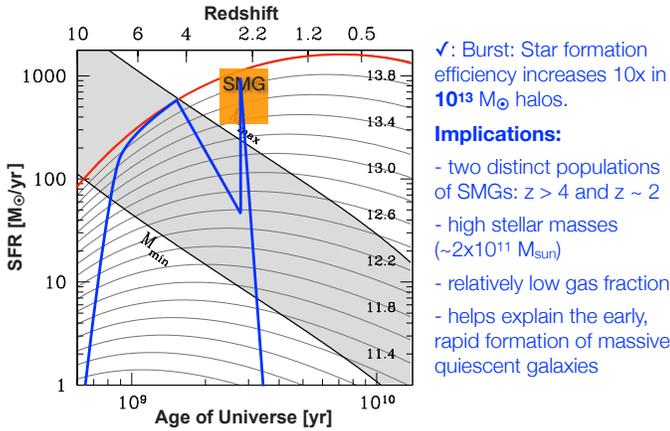
Xue, Fu+2018

The Unsustainable Growth of SMGs

- ▶ $M_{\text{gas}}/\text{SFR} \sim 100$ Myr
- ▶ 10x greater SFR for any given gas mass
- ▶ 10x shorter gas depletion timescale than normal star-forming galaxies
- ▶ Without continuous gas supply, SFR will decline with an e-folding timescale of ~ 200 Myr



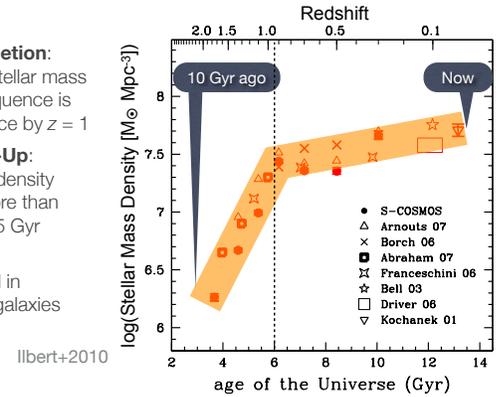
So, what's up with the SMGs?



The early & rapid build-up of the red sequence

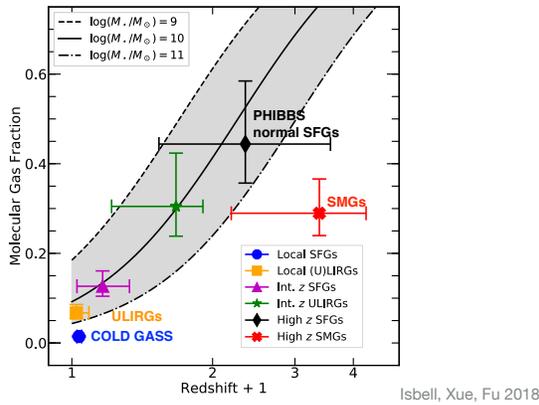
the evolution of the total comoving stellar mass density of quiescent galaxies

- **Early Completion:** Most of the stellar mass in the red sequence is already in place by $z = 1$
- **Rapid Build-Up:** Stellar mass density increased more than 20x in just 2.5 Gyr ($1 < z < 2$).
- **Not observed in** star-forming galaxies



SMGs have lower gas fraction than normal SFGs?

Data Points: gas fractions measured w/ Tully-Fisher relation & $\alpha_{CO} = 1$
Curves: gas fractions inferred from sSFR(z) of different stellar masses



one stone two birds

- SMGs have $\sim 10x$ higher SF efficiency than normal galaxies, i.e., they are massive starbursts
 - Starbursts can stop star formation by rapidly exhausting the gas reservoir, providing a quenching mechanism to turn **blue starforming galaxies** into **red passive galaxies**.
 - Starbursts are a universal phase in the formation of massive red galaxies. All galaxy formation models should be able to reproduce this important phase.
- *What triggers the high star formation efficiency? Why every massive galaxy goes through a burst phase?*

Astronomy originated from and is almost entirely driven by observation, which itself is driven by technological advances!

Tycho's mural quadrant



1577

Galileo's telescope



1610

Hubble in Palomar



1948

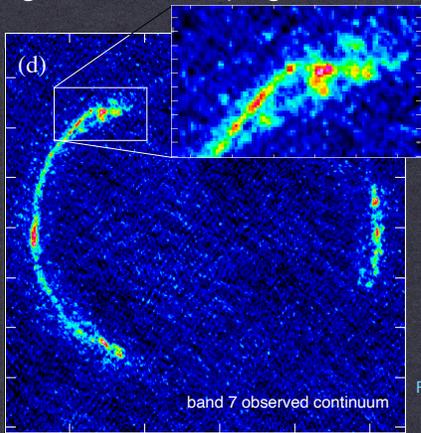
ALMA Inauguration Heralds New Era of Discovery

Revolutionary telescope will enable unprecedented views of the cosmos

13 March 2013

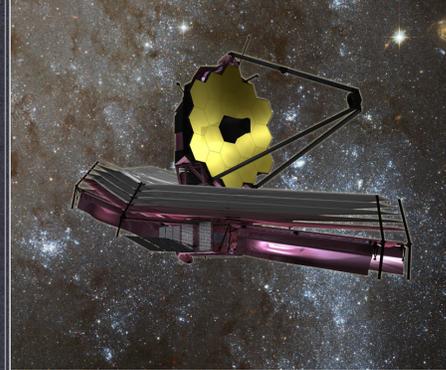


ALMA Long Baseline Campaign: SDP.81 ($z = 3.04$)



ALMA
Partnership 2015
Dye+2015
(23mas=180 pc)

JWST 6.5m (\$10B)
L2 orbit



TMT 30m (\$1B)
alt. 4200 m



SPICA 3.5m
L2 orbit

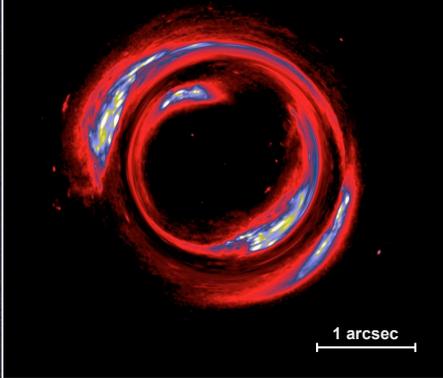


CCAT 25m
alt. 5600 m



Future IR/Submm Telescopes

Simulated Image of Lensed "NGC6090" at $z = 4$



1 arcsec

NGC6090 seen by HST



Put this local interacting luminous IR Galaxy NGC 6090 to $z=4.0$, and place a lensing galaxy at $z=1.5$.

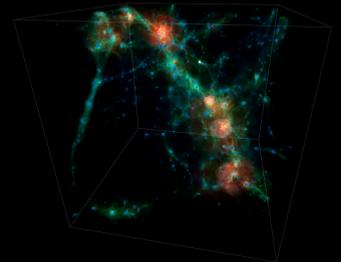
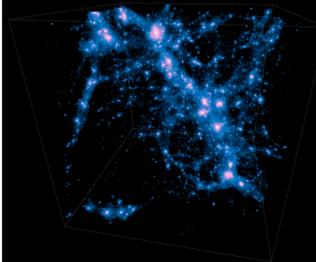
- Seeing: 0.5 arcsec
- HST at $2 \mu\text{m}$: 0.2 arcsec
- JWST at $2 \mu\text{m}$: 0.077 arcsec
- TMT at $2 \mu\text{m}$: 0.017 arcsec

Grav. Lensing + Next Gen Scopes

Cosmological N-body + Hydrodynamical Simulation of Galaxy Formation and Evolution

Dark Matter

Gas Temperature



redshift : 1.54
Time since the Big Bang: 4.3 billion years

stellar mass : 27.7 billion solar masses

ILLUSTRIS