

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} + \mu_0 \mathbf{J}$$



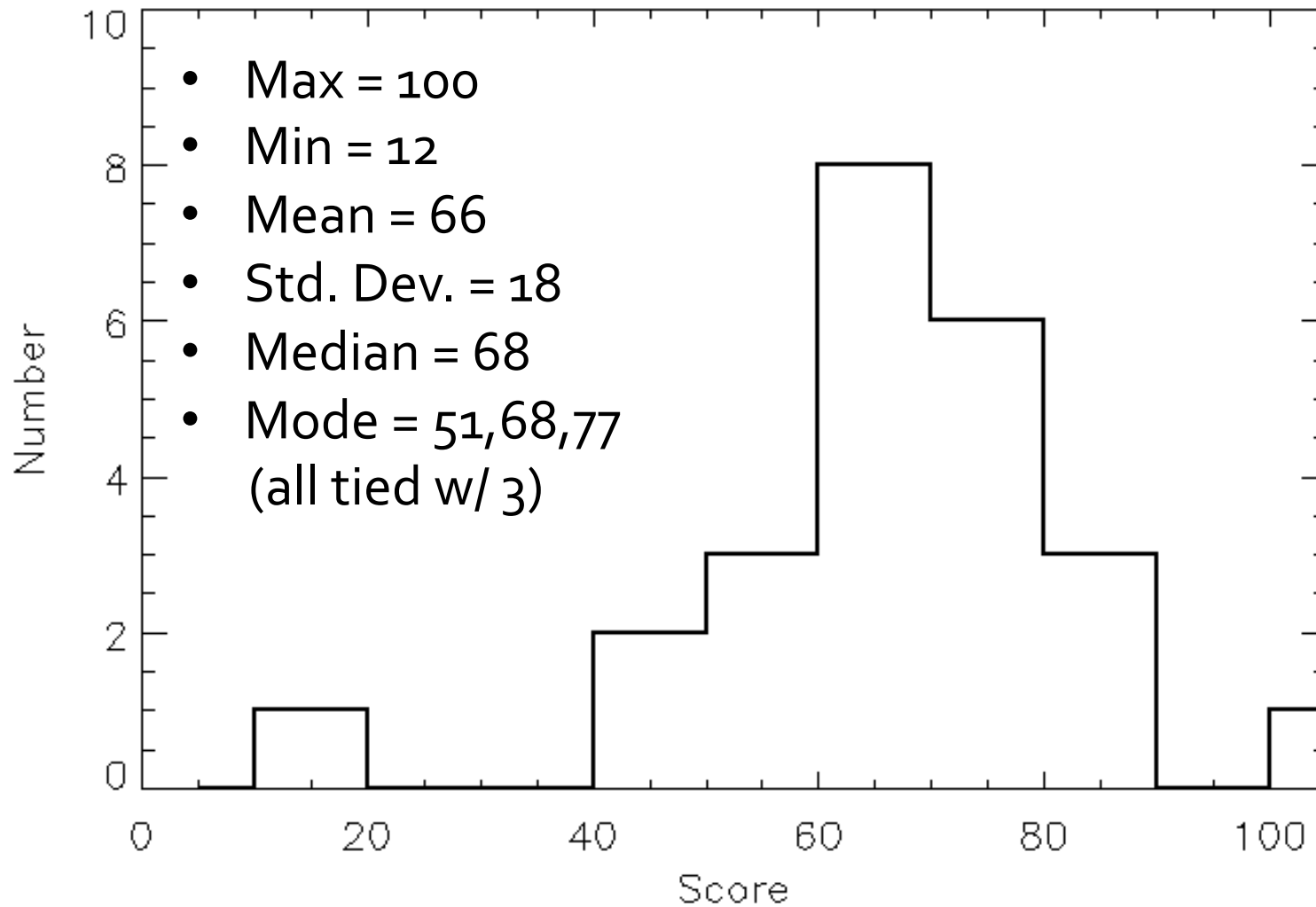
Electricity and Magnetism I: 3811

Professor Jasper Halekas
Van Allen 301
MWF 9:30-10:20 Lecture

Announcements

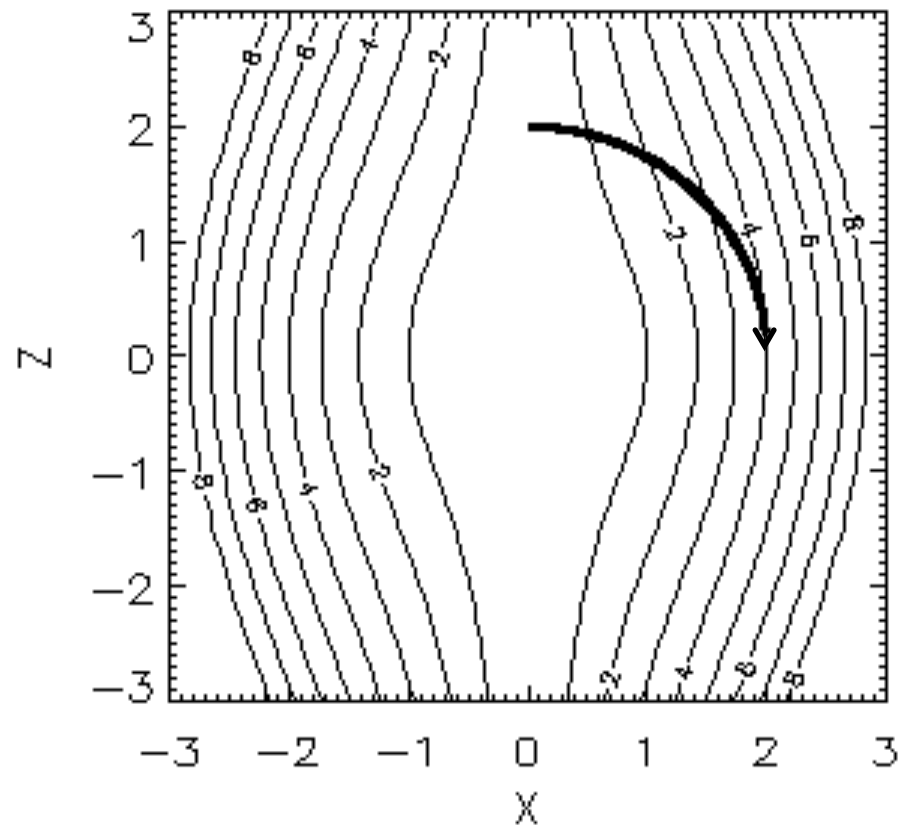
- I will be absent next Monday & Wednesday
 - Prof. Baalrud will substitute
- There is homework due next Friday

Midterm #1



Q1

- Line integrals
- Spherical coordinates
- Gradient theorem

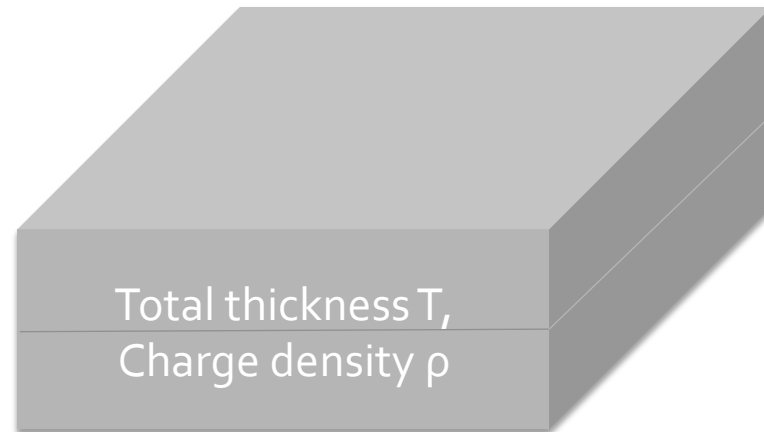


Q2

- Integrating over a delta function picks out the value of the multiplying function at the location of the delta function

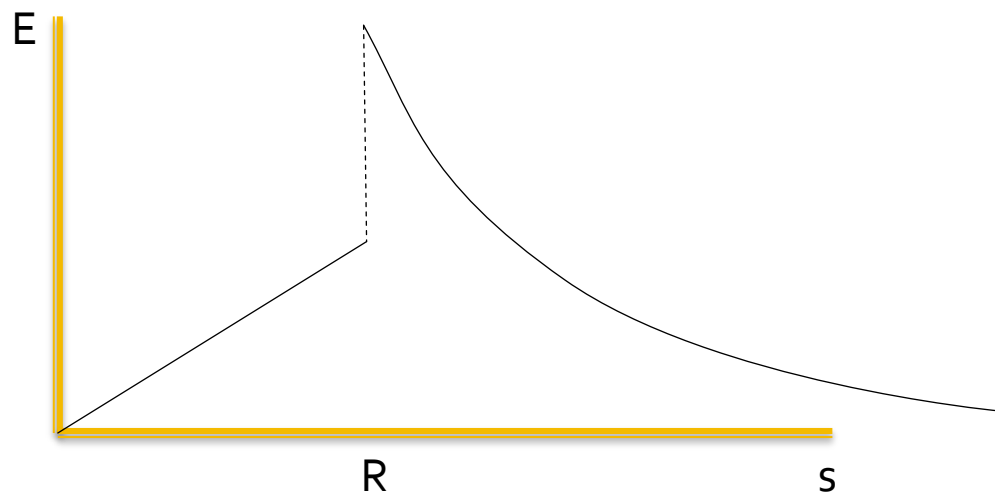
Q3

- Gauss's law:
Integral form
- Cartesian
coordinates
- Potential & work



Q4

- Gauss's law:
Differential
form
- Cylindrical
coordinates
- Boundary
conditions



General Eqs. for \vec{E}, V

$$\left. \begin{aligned} \vec{E}(\vec{r}) &= \frac{1}{4\pi\epsilon_0} \int \frac{\hat{\Delta r}}{\Delta r^2} \rho(\vec{r}') d\tau' \\ V(\vec{r}) &= \frac{1}{4\pi\epsilon_0} \int \frac{1}{\Delta r} \rho(\vec{r}') d\tau' \end{aligned} \right\} \text{Cumbersome!}$$

Gauss's Law: $\nabla \cdot \vec{E} = \rho/\epsilon_0$

\Rightarrow Poisson's Eq. $\nabla^2 V = -\rho/\epsilon_0$

Charge-free Region

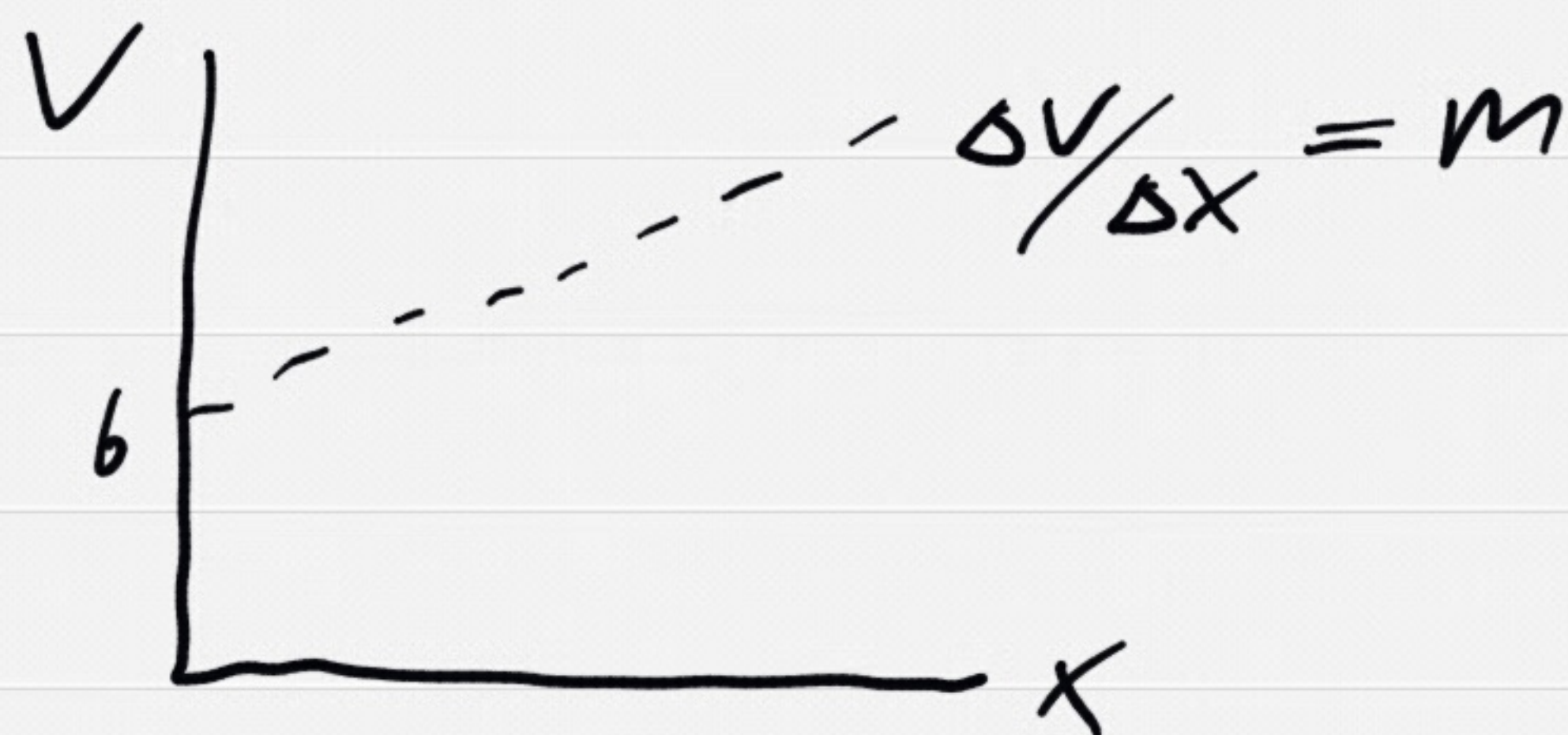
\Rightarrow Laplace's Eq. $\nabla^2 V = 0$

Cartesian:

$$\nabla^2 V = \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0$$

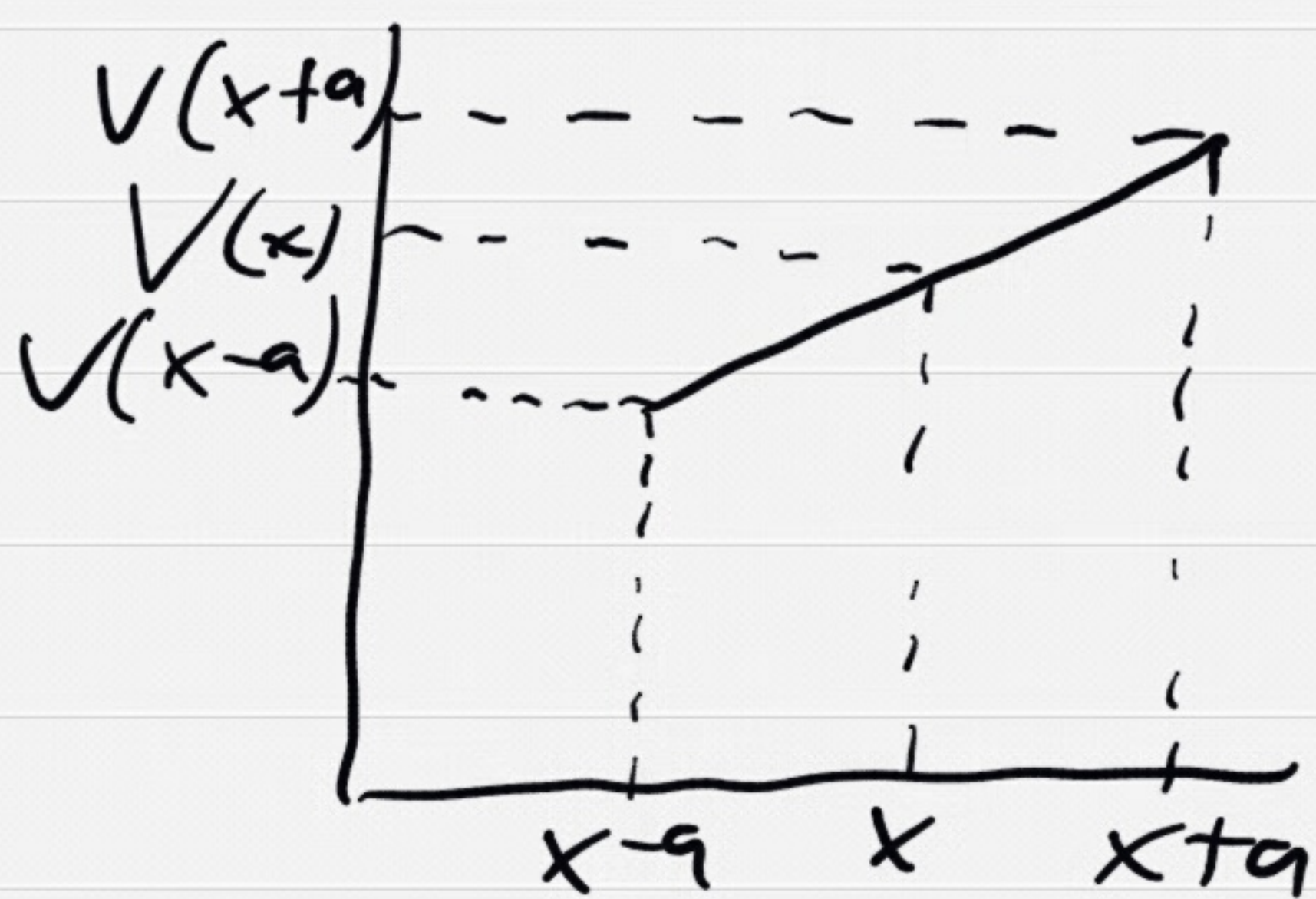
Laplace's Eq. in 1-D

$$d^2V/dx^2 = 0 \Rightarrow V(x) = mx + b$$



Interesting Fact:

$$V(x) = \frac{1}{2} [V(x-a) + V(x+a)]$$



$$\begin{aligned} V(x) &= \frac{1}{2} [V(x-a) + V(x+a)] \\ &= \frac{1}{2} [m(x-a) + b + m(x+a) + b] \\ &= mx + b // \end{aligned}$$

Zero curvature \Rightarrow

No local extrema
(except at endpoints)

Laplace's Eq. In 2-d

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = 0$$

$$V(x, y) = \frac{1}{2\pi R} \oint V dl$$

around a circle centered
at (x, y)

- V has no local extrema
except on boundaries

Laplace's Equation

