Outline

- Go over problems 5-1, 5-2
- Gas heating and cooling
- Critical density
- Emission from HII regions
- Measuring temperature with spectral lines

Gas Cooling

- "Cooling" = energy loss from a system.
- Cooling occurs via radiation of photons:
 - $< 10^3 \text{ K} \rightarrow \text{molecular line emission}$
 - − $10^3 10^4 \text{ K} \rightarrow \text{optical lines of neutral and low-ionization metals}$
 - 10^4 − 10^5 K → H and He recombination
 - − $10^5 10^6 \text{ K} \rightarrow \text{UV}$ and X-ray lines of high-ionization metals
 - $> 10^7 \text{ K} \rightarrow \text{bremmstrahlung}$ (free-free) emission
- "Cooling" does not necessarily mean a decrease in temperature or the kinetic energy of the gas, since cooling can mainly represent release of energy via recombination.
- Cooling function = rate of energy loss per unit volume as a function of temperature of gas. Depends on metallicity and gas excitation mechanism (collisional versus photoionization).

Cooling Function



Boltzmann factor

- Consider two energy levels of an atom or ion.
- Number density in level $1 = n_1$, in level $2 = n_2$. Also called population of a level.
- Statistical weight = g_i = number of distinct quantum states of an energy level, e.g. due to electron spin or orbital angular momentum.
- Boltzmann factor gives ratio of populations:

$$\frac{n_2}{n_1} = \frac{g_2}{g_1} e^{-\Delta E/kT}$$

- To produce photons $hv = \Delta E$, need $hv \sim kT$
- E.g. for T ~ 20,000 K, kT ~ 2 eV, Balmer emission is strongest



Critical Density

• Two levels, gas loses energy by line emission

– Rate = $R_{21,rad} = n_2 A_{21}$ where A_{21} = spontaneous Einstein coefficient

− $A_{21} = 1/(\text{mean life time for decay 2} \rightarrow 1)$.

• Gas is excited by collisions of electrons with ions

– Rate = $R_{12,coll} = n_e n_1 q_{12}$ where q_{12} = collisional excitation coefficient

- $q = q(T) = \langle \sigma v \rangle$ is like recombination coefficient $\alpha(T)$, units = cm³ s⁻¹

- Note
$$n = n_1 + n_2$$
, so $R_{12,coll} = n_e (n - n_2) q_{12}$

• Also have collisional de-excitations

- Rate =
$$R_{21,coll} = n_e n_2 q_{21}$$

• In equilibrium, $R_{12,coll} = R_{21,coll} + R_{21,rad}$

$$n_e(n-n_2)q_{12} = n_2n_eq_{21} + n_2A_{21} \rightarrow n_2 = \frac{n_enq_{12}}{n_e(q_{21}+q_{12}) + A_{21}}$$

Critical Density

• Luminosity in the line emission (per unit volume) is

 $- L_{21} = n_2 A_{21} h v$

$$L_{21} = \frac{n_e n q_{12} A_{21} h \nu}{n_e (q_{21} + q_{12}) + A_{21}} = \frac{n_e n q_{12} h \nu}{(1 + q_{12}/q_{21}) n_e / n_{crit} + 1}$$

where $n_{crit} = A_{21}/q_{21}$

- Note $R_{21,rad} = n_2 A_{21}$ and $R_{21,coll} = n_e n_2 q_{21}$,
 - so $R_{21,rad} / R_{21,coll} = n_2 A_{21} / n_e n_2 q_{21} = A_{21} / n_e q_{21}$
 - set $R_{21,rad} / R_{21,coll} = 1$ and find $n_e = n_{crit} = A_{21} / q_{21}$
 - density where radiative and collisional deexcitation have same rate

Critical Density

- Look at $q_{_{12}}$ / $q_{_{21}}$, consider case with no radiative decay
- In equilibrium $R_{21,coll} = n_e n_2 q_{21} = R_{12,coll} = n_e n_1 q_{12}$, so $q_{12} / q_{21} = n_2 / n_1$
- use Boltzmann factor $\frac{q_{12}}{q_{21}} = \frac{n_2}{n_1} = \frac{g_2}{g_1} e^{-\Delta E/kT} \lesssim 1$
- Back to line luminosity $L_{21} = \frac{n_e n q_{12} h v}{(1 + q_{12}/q_{21}) n_e/n_{crit} + 1}$

• For $n_{\rm e} << n_{\rm crit}$ find $L_{21} \propto n_{\rm e} n \propto n^2$

- For $n_{\rm e} >> n_{\rm crit}$ find $L_{21} \propto n$
- For hydrogen recombination and bremsstrahlung, $L \propto n^2$
- Thus hydrogen recombination and bremsstrahlung dominate at high *n*.

H II regions



- Photons E > 13.6 eV can ionize H
 - ionization σ is high, $\sigma \sim 6.3 \times 10^{\text{-18}} \ cm^2$
 - photons are absorbed $r < r_{strom}$
- Photons E < 13.6 eV cannot ionize H
 - interact with free electrons (Thomson)
 - $\sigma = 6.7 \times 10^{-25} \text{ cm}^2 \text{ is low}$
 - mean free path l ~ $1/n\sigma$ ~ 50 pc > r_{strom}
- Emitted spectrum is *not* blackbody
 - high *E* photons absorbed, then re-emitted in cascade ending with Lyman α
 - low E photons escape
 - Lyman α random walks to edge of region
 - photons from metals also escape
- Gas inside *is* in thermal equilibrium with itself, but not with radiation.

Oxygen Line Emission

• For [O III], critical density $\sim 10^6$ cm⁻³.

t'

- Density is sufficiently low that [O III] lines had never been seen in a laboratory before they were found astronomically, initial conclusion was existence of a new element "nebulium".
- At low densities, [O III] is a dominant cooling mechanism.



Measuring the Temperature

- Luminosity in λ 4363 line $\propto n({}^{1}S_{0})$
- $L(\lambda 4959) + L(\lambda 5007) \propto n(^{1}D_{2})$
- Boltzmann factor

$$\frac{n_S}{n_D} = \frac{g_S}{g_D} e^{-\Delta E/kT}$$

• Can determine $n({}^{1}S_{0})$ and $n({}^{1}D_{2})$ from L(λ 4363) and L(λ 4959)+L(λ 5007) with corrections for Einstein coefficients and statistical weights. In low *n* limit, find

$$\frac{L_{\lambda 4959} + L_{\lambda 5007}}{L_{\lambda 4363}} = \frac{7.90 \exp(3.29 \times 10^4 T)}{1 + 4.5 \times 10^{-4} n_e / T^{1/2}}$$



Measuring the Temperature



• Spectrum of HeIII region surrounding an X-ray binary in the galaxy NGC 5408 (Kaaret & Corbel 2009).

Homework

- For next class:
 - Problem 5-3