

# HW #13

1)  $\lambda = 1, 1, 4$

2)  $e^{ax}$   $\lambda = a^2$   $a, k$  are real numbers

$\sin kx$   $\lambda = -k^2$

$\cos kx$   $\lambda = -k^2$

3)  $M = \begin{pmatrix} 1 & 1 \\ 1 & 3 \end{pmatrix}$   $\lambda = 2 \pm \sqrt{2}$

$\lambda_1 = 2 + \sqrt{2}$   $v_1 = \begin{pmatrix} -1 + \sqrt{2} \\ 1 \end{pmatrix}$   $\lambda_2 = 2 - \sqrt{2}$   $v_2 = \begin{pmatrix} -1 - \sqrt{2} \\ 1 \end{pmatrix}$

$P = \begin{pmatrix} -1 + \sqrt{2} & -1 - \sqrt{2} \\ 1 & 1 \end{pmatrix}$

$A = \begin{pmatrix} \sqrt{2} & -\sqrt{2} \\ 2 + \sqrt{2} & 2 - \sqrt{2} \end{pmatrix}$

$P^{-1} = \frac{1}{2\sqrt{2}} \begin{pmatrix} 1 & 1 + \sqrt{2} \\ -1 & -1 + \sqrt{2} \end{pmatrix}$

$B = \begin{pmatrix} 2 + \sqrt{2} & 0 \\ 0 & 2 - \sqrt{2} \end{pmatrix}$

Yes,  $B = \begin{pmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{pmatrix}$

$v_1 \cdot v_2 = 0$