



## L-14 Fluids - 3

- **Fluids at rest** → Fluid Statics  
Why things float → *Archimedes' Principle*
- **Fluids in Motion** → Fluid Dynamics
  - Hydrodynamics
  - Aerodynamics

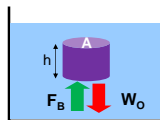
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**Example:** What does 1 liter (about a quart) of water weigh?

- 1 liter = 1000 cm<sup>3</sup>
- Density of water = 1 g/cm<sup>3</sup> = 1000 kg/m<sup>3</sup>
- Mass of 1 liter of water  
= 1 g/cm<sup>3</sup> x 1000 cm<sup>3</sup> = 1000 g = 1 kg
- $W = mg = 1 \text{ kg} \times 9.8 \text{ m/s}^2 = 9.8 \text{ N} (\approx 10 \text{ N})$   
= 2.2 pounds (1 gallon → 8 pounds)
- **Water weighs about 10 N/liter**

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## Archimedes principle



- ♦ The buoyant force on an object in a fluid equals the *weight of the fluid (e.g., water) which it displaces*.
- ♦ Anything less dense than water will float in water
- ♦ water weighs 10N/liter → each liter of displaced water provides 10 N of buoyant force

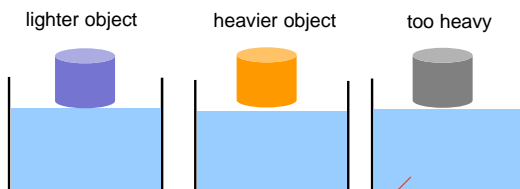
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## Will it float?

- The buoyant force is always there whether the object floats or not
- The object will float if the buoyant force is big enough to support the object's weight
- The object will displace just enough water so that the buoyant force = its weight
- If the object is completely submerged, and the weight of the displaced water is less than the weight of the object, the object will sink
- **Objects that have a density less than water will float**- when fully submerged, they weigh less than the water, so the water supports them
- An object will float in a liquid that is denser than it;  
→ a steel bolt will float in mercury

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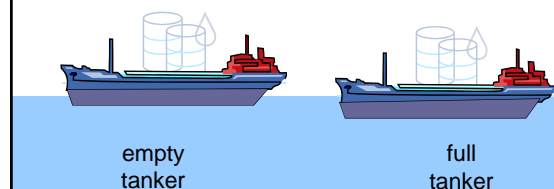
## Floating or sinking objects



The weight of displaced water is less than the weight of the object

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## Oil Tankers

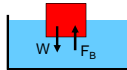


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### example problem

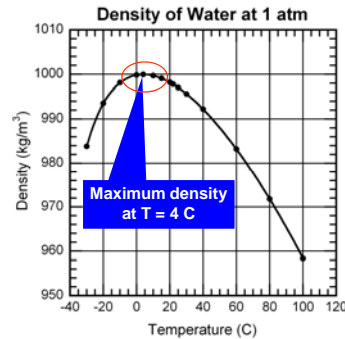
- An object having a volume of 6 liters and weighing  $W = 30 \text{ N}$  is placed in a tank of water. *What will happen? Will it sink? Will it float? What fraction of its volume will be submerged if it floats?*
- If the object were completely submerged, the buoyant force would be  

$$F_{B, \text{max}} = 10 \text{ N/liter} \times 6 \text{ liters} = 60 \text{ N}$$
- thus, the object will float with *half* of its volume submerged, so that  $F_B = W = 30 \text{ N}$



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### Water is weird stuff!



The pressure of expanding ice can break steel pipes.

[VIDEO](#)

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### Why does ice float?

- Water, the most plentiful substance on earth is also one of the most unusual in its behavior in that it *expands when it freezes*.
- Since it expands, the density of ice is slightly less than the density of water ( $958 \text{ kg/m}^3$  as compared to  $1000 \text{ kg/m}^3$  for water). So the part of the iceberg above the surface contains less than 10 % of the total volume.



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### Fluid Flow → fluid dynamics

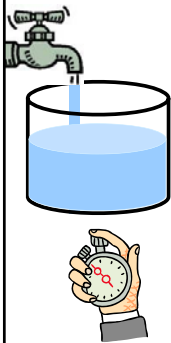


Daniel Bernoulli

- A Swiss mathematician, born in 1700.
- He applied the laws of mechanics to the problem of fluid flow
- He developed the basic principle that explains, for example, how airplanes work

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### How do we measure fluid flow?

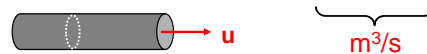


- We can time how long it takes to fill a bucket, say 30 seconds
- the flow rate is then 1 bucket say per 30 seconds
- in other words, the flow rate is **volume of fluid per unit time**
- gallons per min (gpm), liters/s, cubic feet per min (cfm), or  $\text{m}^3/\text{s}$
- $Q_v = \text{volume flow rate}$

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### Volume flow rate → $Q_v$

- If the water comes out of a tube of cross sectional area  $A$  with a flow speed  $u$  the volume flow rate =  $Q_v = u \times A \text{ (m/s} \times \text{m}^2\text{)}$



- To measure  $u$  just see how long it takes to fill a gallon jug from a hose and measure the diameter of the hose.

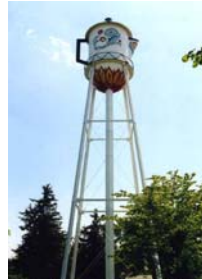
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## Mass flow rate $\rightarrow Q_m$

- We could also measure how much mass comes out per unit time – **kg/s** for example
- if you are using a fluid of density  $\rho$  coming out of a hose of cross sectional area  $A$  with speed  $v$  the mass flow rate is
- **mass flow rate** =  $Q_m = \rho \times u \times A = \rho Q_v$

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## What makes water flow?



**Stanton, IA**  
**Montgomery Co. Pop. 680**

- gravity
- by placing the water up high, the pressure at the bottom is high enough to supply water to all parts of town that are lower than the tower

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## Pressure differences



- Water experiences a **resistance** to flow
- a **pressure difference** must be maintained across the ends of the pipe to push the water along  $\rightarrow$   **$P_2$  must be greater than  $P_1$**
- this pressure difference can be maintained by a water pump

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## Water does not disappear!

- If water goes in one end of a pipe it must come out the other end (if there are no leaks). Sounds obvious, but it has a number of interesting consequences!
- **This applies to pipes that have constrictions**



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## Principle of the continuity of flow

- since whatever goes in must come out, we have that the incoming flow rate – outgoing flow rate or,  $Q_{v1} = Q_{v2}$   
 $\rightarrow v_1 A_1 = v_2 A_2$  (**continuity principle**)
- thus the fluid in the narrow part of the tube must flow **FASTER** than the fluid on the left.
- Cardiologists use this to determine if arteries might be clogged.

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## Other examples - the nozzle effect



- you use this principle whenever you hold your finger over the end of the hose to make the water spray farther.



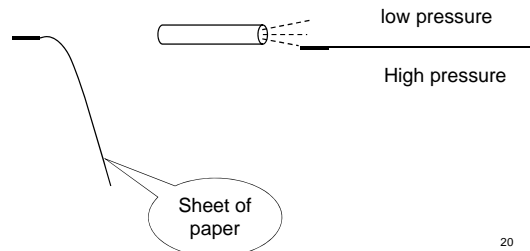
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### An amazing thing about moving fluids

- The pressure in a moving fluid is less than the pressure in a fluid at rest → this is **Bernoulli's Principle**
- Where a fluid moves faster its pressure is lower, where it moves slower, its pressure is higher
- As we will see, this is the principle that allows airplanes to fly

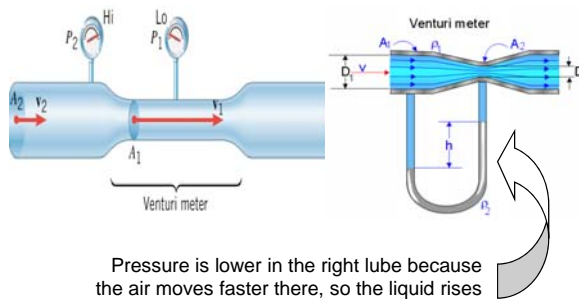
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### You can demonstrate Bernoulli's principle with a sheet of paper!



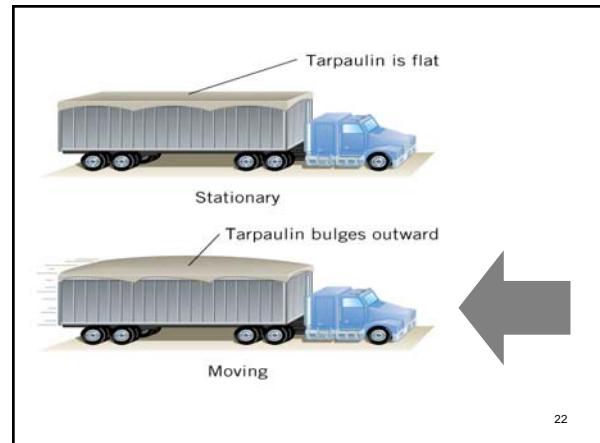
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### The Venturi Meter



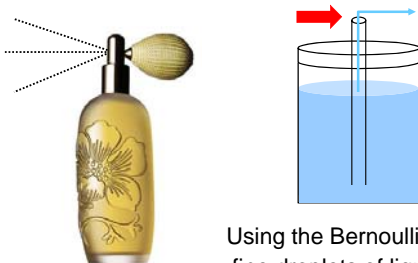
Pressure is lower in the right lube because the air moves faster there, so the liquid rises

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### Atomizers (perfume spritzers)



Using the Bernoulli effect, fine droplets of liquid are formed with this device

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