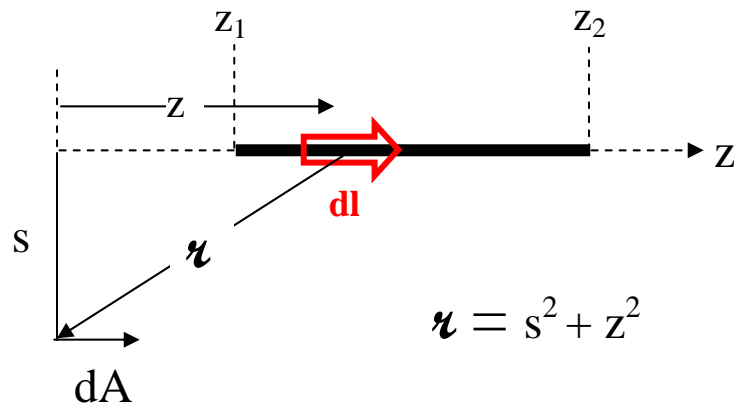


Griffiths 5.22 (Magnetic vector potential for a finite wire)

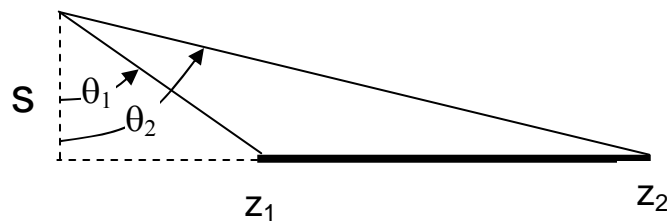


$$\vec{A}(\vec{r}) = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{l}}{r} = \frac{\mu_0 I}{4\pi} \int_{z_1}^{z_2} \frac{dz}{\sqrt{s^2 + z^2}} \hat{z} = \frac{\mu_0 I}{4\pi} \ln \left[\frac{z_2 + \sqrt{s^2 + z_2^2}}{z_1 + \sqrt{s^2 + z_1^2}} \right] \hat{z}$$

$$\vec{B} = \nabla \times \vec{A} = -\frac{\partial A_z}{\partial s} \hat{\phi} = -\frac{\mu_0 I}{4\pi} \left[\frac{s(s^2 + z_2^2)^{-1/2}}{z_2 + \sqrt{s^2 + z_2^2}} - \frac{s(s^2 + z_1^2)^{-1/2}}{z_1 + \sqrt{s^2 + z_1^2}} \right] \hat{\phi}$$

$$\vec{B} = -\frac{\mu_0 I}{4\pi} \left[\frac{s(s^2 + z_2^2)^{-1/2}}{z_2 + \sqrt{s^2 + z_2^2}} \left(\frac{z_2 - \sqrt{s^2 + z_2^2}}{z_2 - \sqrt{s^2 + z_2^2}} \right) - \frac{s(s^2 + z_1^2)^{-1/2}}{z_1 + \sqrt{s^2 + z_1^2}} \left(\frac{z_1 - \sqrt{s^2 + z_1^2}}{z_1 - \sqrt{s^2 + z_1^2}} \right) \right] \hat{\phi}$$

$$\vec{B} = \frac{\mu_0 I}{4\pi s} \left[\frac{z_2}{\sqrt{s^2 + z_2^2}} - \frac{z_1}{\sqrt{s^2 + z_1^2}} \right] \hat{\phi}$$



$$\vec{B} = \frac{\mu_0 I}{4\pi s} [\sin(\theta_2) - \sin(\theta_1)] \hat{\phi}$$