

1.a.  $\rightarrow \vec{B} = \mu_0 n I_s \hat{z}$
 $= \mu_0 n k t \hat{z}$

$$\begin{aligned} \mathcal{E}_{ind} &= -d\Phi_B/dt \\ &= -d/dt (B \cdot \pi a^2) \\ &= -\pi a^2 dB/dt \\ &= -\pi a^2 \cdot \mu_0 n \cdot dI_s/dt \\ &= \boxed{-\pi a^2 \cdot \mu_0 n \cdot k} \quad \text{CCW} \end{aligned}$$

b. $I_c(t) = \mathcal{E}/R = (V_0 + \mathcal{E}_{ind})/R$
 $= \boxed{(V_0 - \pi a^2 \mu_0 n \cdot k)/R}$

2a. $\vec{E} = -\nabla V$ Note: $L = h$
 $= \Delta V/L \hat{z} = \boxed{V_0 \sin(\omega t)/L \hat{z}}$

b. $\oint \vec{B} \cdot d\vec{l} = \mu_0 \epsilon_0 d/dt \int \vec{E} \cdot d\vec{a}$
 $B \cdot 2\pi s = \mu_0 \epsilon_0 d/dt \frac{V_0 \sin(\omega t) \cdot \pi s^2}{L}$

$$\Rightarrow \boxed{\vec{B} = \frac{\mu_0 \epsilon_0 \omega V_0 \cos(\omega t) \cdot s}{2L} \hat{\phi}}$$

2c. $\vec{S} = \frac{1}{\mu_0} (\vec{E} \times \vec{B})$
 $= \frac{1}{\mu_0} \cdot \frac{V_0 \sin(\omega t)}{L} \cdot \frac{\mu_0 \epsilon_0 \omega V_0 \cos(\omega t) s}{2L} \hat{z} \times \hat{\phi}$
 $= \boxed{-\frac{\epsilon_0 \omega V_0^2 \sin(\omega t) \cos(\omega t) s}{2L^2} \hat{s}}$

$$\begin{aligned}
 2d. \quad u &= \frac{1}{2} \epsilon_0 E^2 + \frac{B^2}{2\mu_0} \\
 &= \frac{1}{2} \epsilon_0 \frac{V_0^2 \sin^2(\omega t)}{L^2} + \frac{1}{2\mu_0} \frac{\mu_0^2 \epsilon_0^2 \omega^2 V_0^2 \cos^2(\omega t) s^2}{4L^2} \\
 &= \boxed{\frac{1}{2} \epsilon_0 \frac{V_0^2}{L^2} \left[\sin^2(\omega t) + \left(\frac{\omega}{c}\right)^2 \frac{s^2}{4} \cos^2(\omega t) \right]}
 \end{aligned}$$

$$\begin{aligned}
 2e. \quad u &\sim \frac{1}{2} \epsilon_0 \frac{V_0^2}{L^2} \sin^2(\omega t) \\
 \frac{\partial u}{\partial t} &\sim \epsilon_0 \frac{V_0^2}{L^2} \cdot \omega \sin(\omega t) \cos(\omega t) \\
 -\nabla \cdot \vec{S} &= -\frac{1}{s} \frac{\partial}{\partial s} (s S_s) \\
 &= \frac{\epsilon_0 \omega V_0^2 \sin(\omega t) \cos(\omega t)}{2L^2 s} \frac{\partial}{\partial s} (s^2) \\
 &= \frac{\epsilon_0 \omega V_0^2 \sin(\omega t) \cos(\omega t)}{L^2} = \frac{\partial u}{\partial t} //
 \end{aligned}$$

$$3a. \quad \vec{g} = \epsilon_0 (\vec{E} \times \vec{B}) = \epsilon_0 \left[E_0 \cos(kz - \omega t) \hat{y} \times \frac{E_0}{c} \cos(kz - \omega t) \hat{z} \times \hat{y} \right]$$

$$\begin{aligned}
 \Rightarrow g_0 &= \frac{\epsilon_0 E_0^2}{c} \\
 \text{or } E_0 &= \sqrt{c g_0 / \epsilon_0}
 \end{aligned}$$

$$\begin{aligned}
 S_0 \quad \vec{E} &= \sqrt{\frac{c g_0}{\epsilon_0}} \cos(kz - \omega t) \hat{y} \\
 \vec{B} &= -\sqrt{\frac{g_0}{c \epsilon_0}} \cos(kz - \omega t) \hat{x}
 \end{aligned}$$

$$\begin{aligned}
 3b. \quad T_{zz} &= \epsilon_0 (E_z E_z - \frac{1}{2} E^2) \\
 &\quad + \frac{1}{\mu_0} (B_z B_z - \frac{1}{2} B^2) \\
 &= -\frac{1}{2} \epsilon_0 E^2 - \frac{B^2}{2\mu_0} \\
 &= -\frac{1}{2} \left[\epsilon_0 \frac{c g_0}{\epsilon_0} + \frac{1}{\mu_0} \frac{g_0}{\epsilon_0 c} \right] \cos^2(kz - \omega t) \\
 &= \boxed{-c g_0 \cos^2(kz - \omega t)}
 \end{aligned}$$

$$3c. \vec{F} = \int T_{zz} \cdot -da_z$$

↑ unit normal
in $-z$

$$= \boxed{A c g_0 \cos^2(kz - \omega t) \hat{z}}$$

Note: There is also a dg/dt term but it averages to zero
I didn't hold it against you if you didn't calculate it.

$$3d. P = \langle F \rangle / A = c g_0 \langle \cos^2(kz - \omega t) \rangle$$

$$= \frac{1}{2} c g_0$$

should have

$$P = \langle S \rangle / c$$

$$= \frac{\langle g \rangle c^2}{c}$$

$$= \langle g \rangle c$$

$$= \frac{1}{2} g_0 c //$$