

College Physics I: 1511

Mechanics & Thermodynamics

Professor Jasper Halekas
Van Allen Lecture Room 1
MWF 8:30-9:20 Lecture

Announcements

- Friday's exam will have randomized seating
 - Pick up your exam (answer sheet inside) before 8:30 and find your seat
 - Sign and print your name on the cover sheet and fill out your name/ID on answer sheet, but don't open the exam until I give you the go-ahead
- Exam is closed-book
 - Calculators are allowed as long as they are not connected to the internet in any way
 - Bring a pencil!
- Bring your ID – it will be checked when you hand in the exam
 - Turn in both answer sheet and signed exam

Announcements II

- Exam is 15 multiple-choice questions
 - Questions are a mix of conceptual and mathematical
 - The intended mean on the exam is ~60%.
 - Don't worry if you can't solve every question.
 - Not every question is equal in difficulty. Be strategic in how you spend your time.
- Exam will cover:
 - Ch. 2-4: All Sections
 - Ch. 5: 5.1-5.3, 5.7 (not 5.4-5.6)
 - Ch. 6: 6.1-6.6 (not 6.7-6.9)

Equation Sheet

Trigonometry (For right triangle with sides Adjacent, Opposite, and Hypoteneuse):

$$\begin{array}{llll} \sin(\theta) = O/H & \cos(\theta) = A/H & \tan(\theta) = O/A & H^2 = O^2 + A^2 \quad A_{\text{circle}} = \pi r^2 \\ \sin(30^\circ) = \cos(60^\circ) = 1/2 & \sin(60^\circ) = \cos(30^\circ) = \sqrt{3}/2 \sim 0.866 & & \sin(45^\circ) = \cos(45^\circ) = \sqrt{2}/2 \sim 0.707 \\ \sin(0^\circ) = \cos(90^\circ) = 0 & \sin(90^\circ) = \cos(0^\circ) = 1 & & \end{array}$$

Kinematics:

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t} \quad \langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t} \quad \vec{r}(t) = \vec{r}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2 \quad v(t)^2 = v_0^2 + 2\vec{a} \cdot \Delta \vec{r}(t)$$

Newton's Laws:

$$\sum \vec{F} = m\vec{a} \quad \vec{F}_{AB} = -\vec{F}_{BA}$$

Forces:

$$\begin{array}{lll} F_G = mg \text{ (@ surface)} & f_s^{MAX} = \mu_s F_N & f_k = \mu_k F_N \\ F_C = ma_c = \frac{mv^2}{r} & F_{\text{spring}} = -kx & \end{array}$$

Work & Energy:

$$\begin{array}{lll} KE_{\text{trans}} = \frac{1}{2}mv^2 & \Delta KE = W_{\text{net}} & PE_G = mgh \quad PE_{\text{spring}} = \frac{1}{2}kx^2 \\ E = KE + PE & \Delta E = W_{nc} & W = \vec{F} \cdot \Delta \vec{r} = |\vec{F}| |\Delta \vec{r}| \cos \theta_{Fdr} \end{array}$$

Rotational Motion:

$$\theta = s/r \quad a_c = \frac{v^2}{r}$$

Basic Trigonometry

Trigonometry (For right triangle with sides Adjacent, Opposite, and Hypoteneuse):

$$\sin(\theta) = O/H$$

$$\cos(\theta) = A/H$$

$$\tan(\theta) = O/A$$

$$H^2 = O^2 + A^2$$

$$A_{\text{circle}} = \pi r^2$$

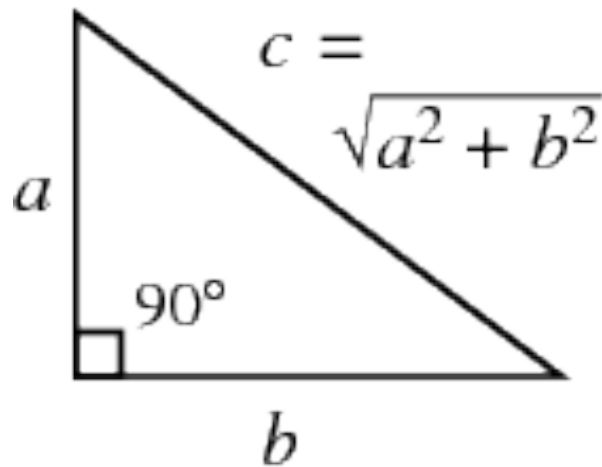
$$\sin(30^\circ) = \cos(60^\circ) = \frac{1}{2}$$

$$\sin(60^\circ) = \cos(30^\circ) = \frac{\sqrt{3}}{2} \approx 0.866$$

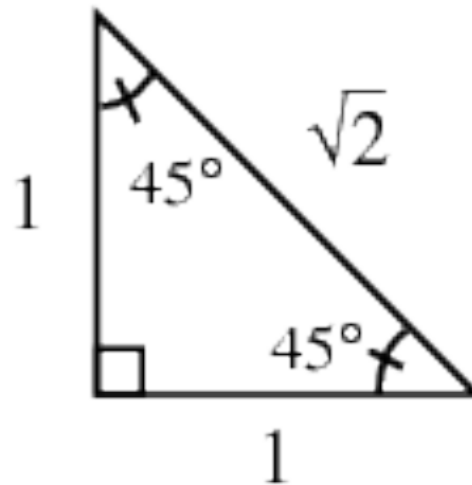
$$\sin(45^\circ) = \cos(45^\circ) = \frac{\sqrt{2}}{2} \approx 0.707$$

$$\sin(0^\circ) = \cos(90^\circ) = 0$$

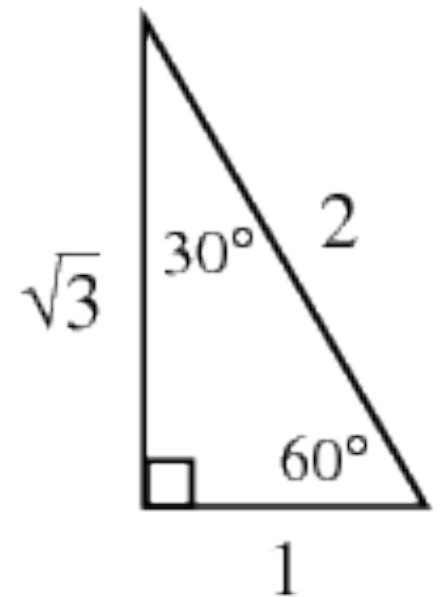
$$\sin(90^\circ) = \cos(0^\circ) = 1$$



*general right
triangle*



*isosceles right
triangle*

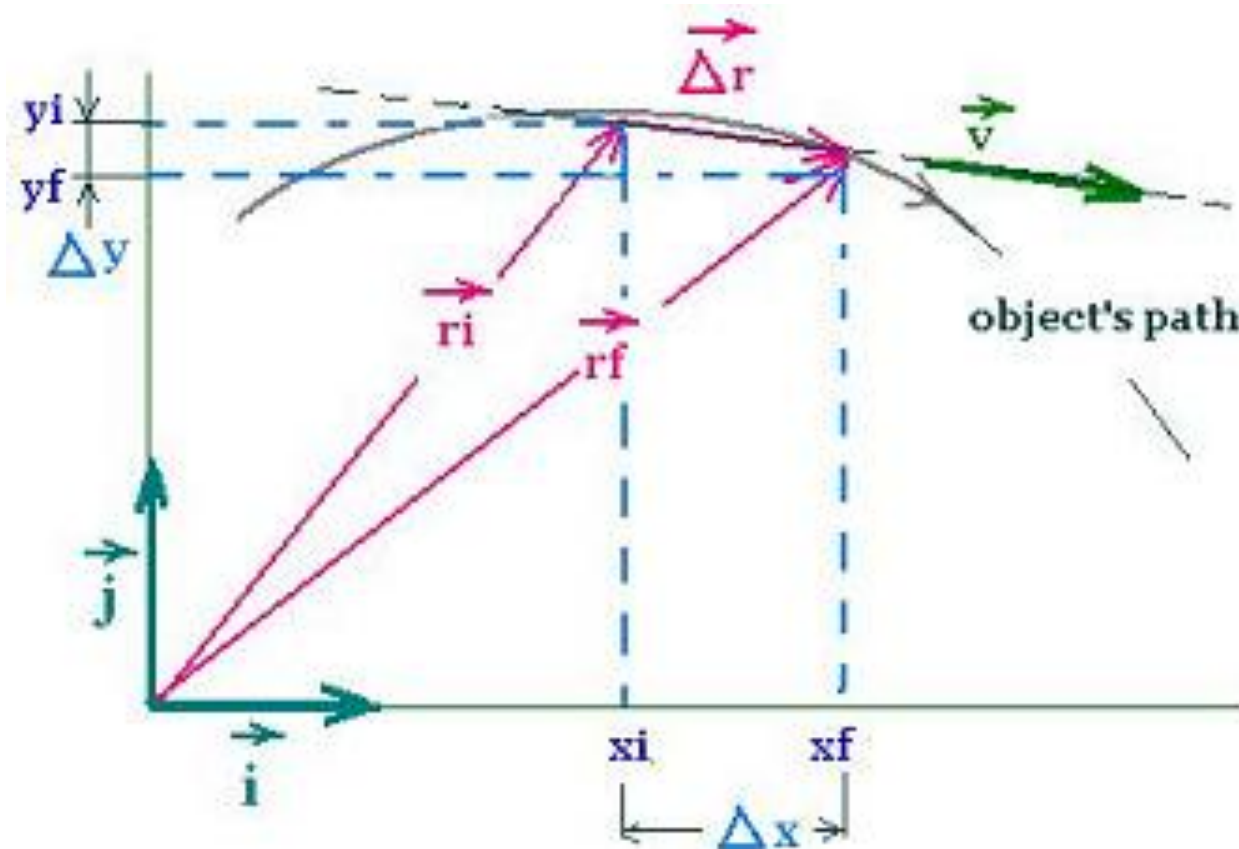


*30-60-90°
triangle*

Kinematics

Kinematics:

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t} \quad \langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t} \quad \vec{r}(t) = \vec{r}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2 \quad v(t)^2 = v_0^2 + 2\vec{a} \cdot \Delta \vec{r}(t)$$



2-d Kinematics

Kinematic Equations

X

I. $v_x = v_{0x} + a_x t$

II. $x = x_0 + v_{0x} t + \frac{a_x}{2} t^2$

III. $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$

Y

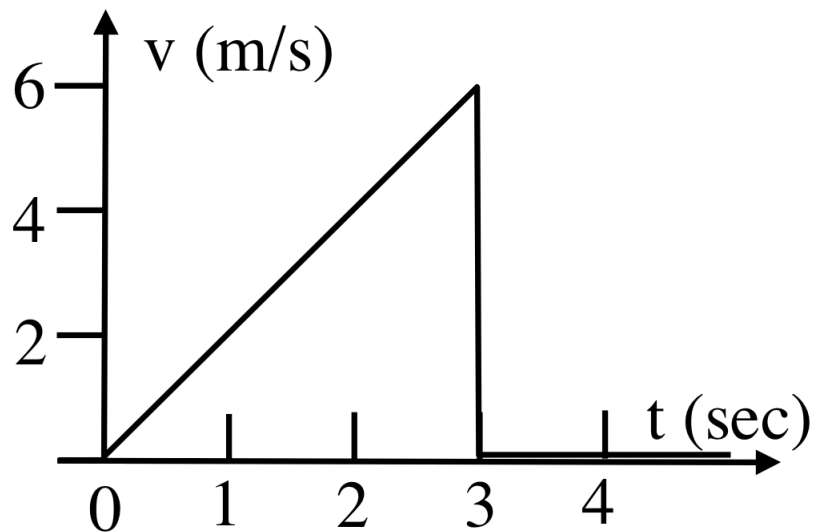
I. $v_y = v_{0y} + a_y t$

II. $y = y_0 + v_{0y} t + \frac{a_y}{2} t^2$

III. $v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$

Sample Question

A particle starts at the origin. Below is a graph of velocity vs. time.



What is the approximate position at $t=3$ sec?

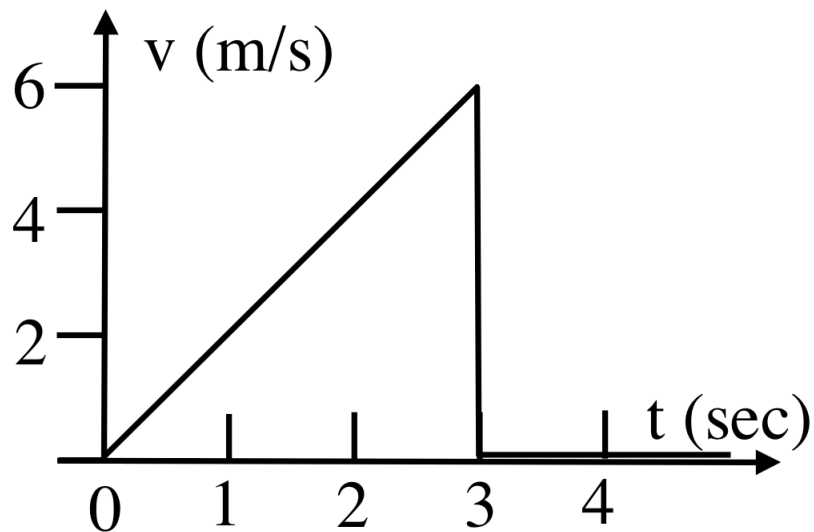
A: 3 m B: 6 m

C: 9 m D: 18 m

E: None of these/not enough information.

Sample Question

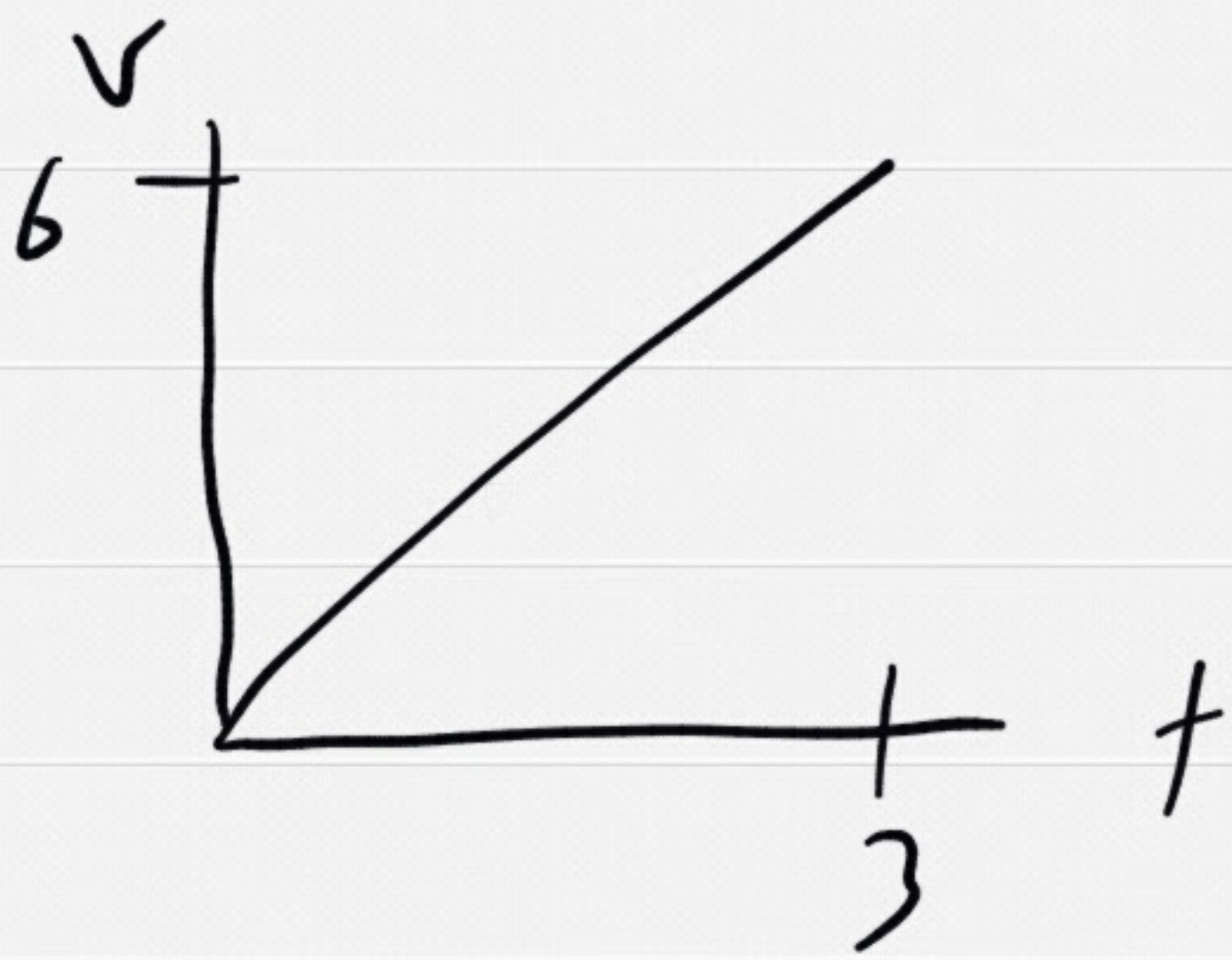
A particle starts at the origin. Below is a graph of velocity vs. time.



What is the approximate position at $t=3$ sec?

- A: 3 m B: 6 m
C: 9 m D: 18 m

E: None of these/not enough information.



$$v = 2t \\ = at \Rightarrow a = 2$$

$$x = x_0 + v \cdot t + \frac{1}{2} a t^2 \\ = \frac{1}{2} a t^2 \\ = \frac{1}{2} \cdot 2 \cdot 3^2 \\ = \boxed{9 \text{ m}}$$

or, see

$$\langle v \rangle = 3 \text{ m/s}$$

$$\Delta x = \langle v \rangle t \\ = 3 \cdot 3 \\ = 9 \text{ m}$$

Sample Question

- A rock is dropped from rest from a height h above the ground. It falls and hits the ground with a speed of 11 m/s. From what height should the rock be dropped so that its speed on hitting the ground is 22 m/s? Neglect air resistance.
- A. $4.0h$
B. $2.0h$
C. $0.71h$
D. $3.0h$
E. $1.4h$

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$$v^2 = v_0^2 + 2a \Delta x$$
$$= 2 \cdot -g \cdot -h = 2gh$$

double v

$$\rightarrow (2v)^2 = 4v^2$$
$$= 4(2gh)$$

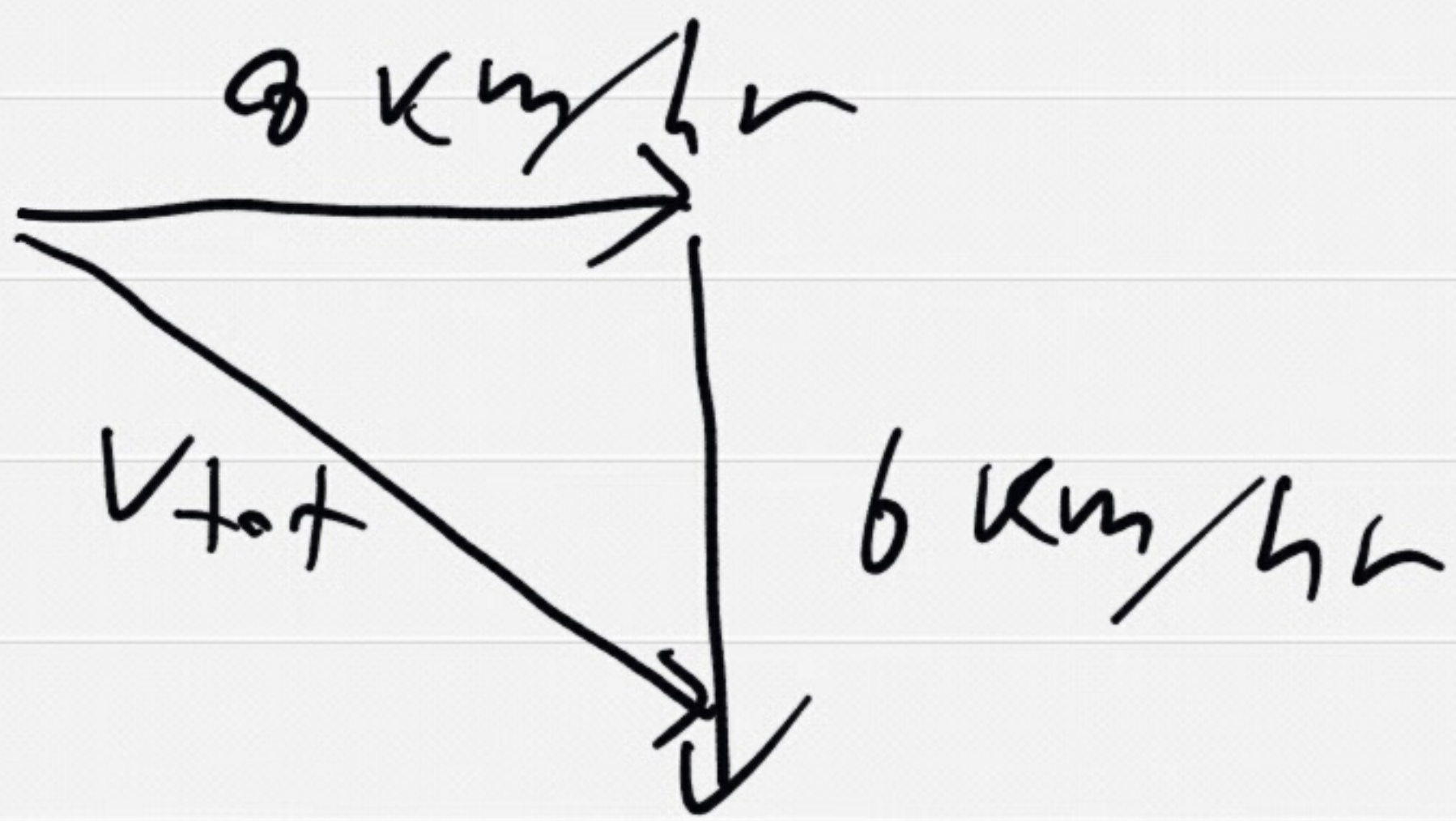
$$\Rightarrow h \rightarrow 4h$$

Sample Question

- A ferry can travel at a speed of 8 km/h in still water, relative to the dock. What is the speed of the ferry, as seen from the dock, if it moves perpendicular to a 6 km/h current that carries it downstream?
 - A. 14 km/h
 - B. 8 km/h
 - C. 28 km/h
 - D. 4 km/h
 - E. 10 km/h

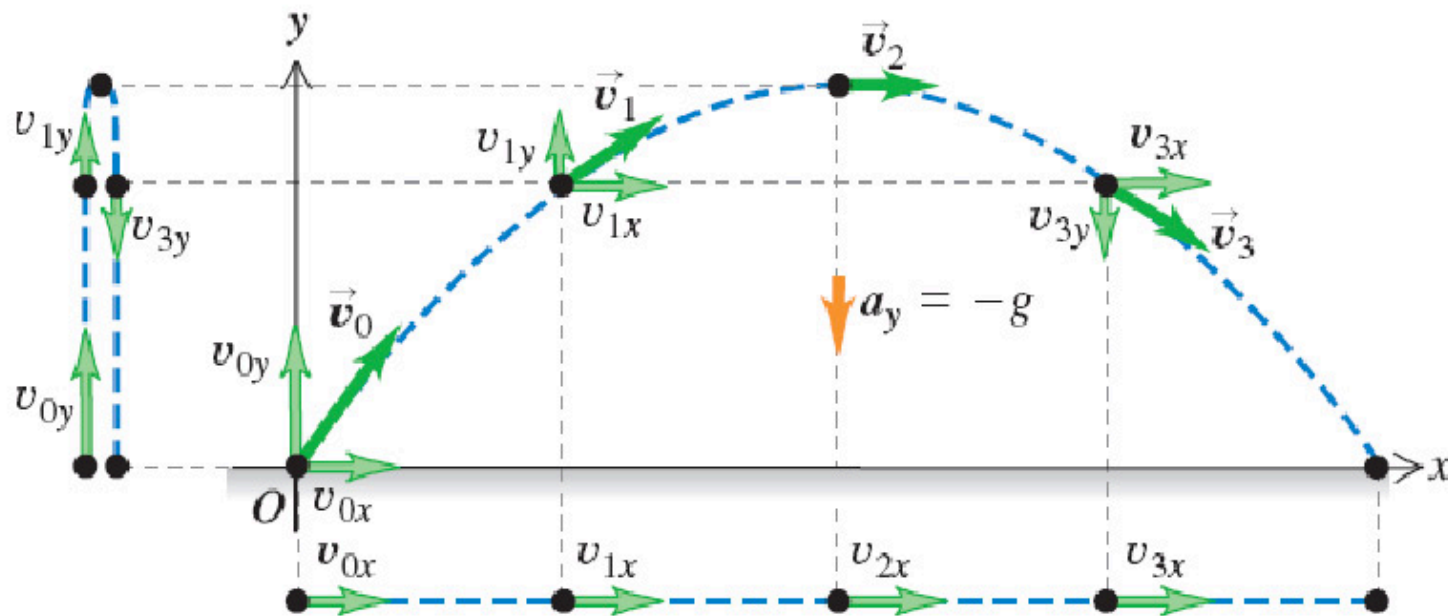
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$$\begin{aligned} V_{tot} &= \sqrt{8^2 + 6^2} \\ &= \sqrt{64 + 36} \\ &= \sqrt{100} \\ &= 10 \text{ km/hr} \end{aligned}$$

Projectile Motion

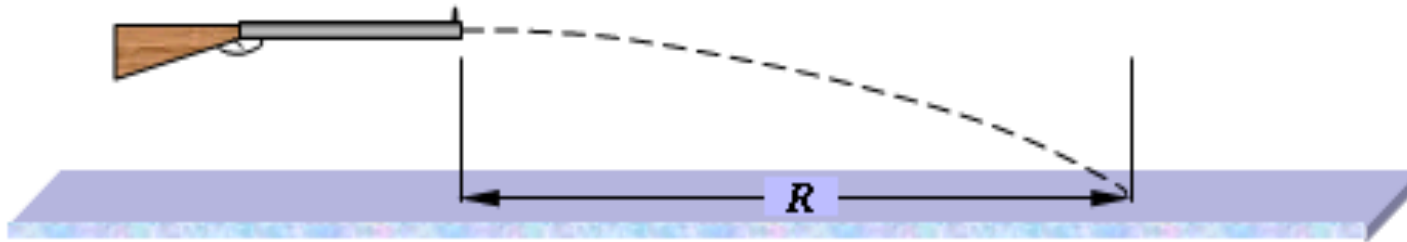


The vertical and horizontal components of a projectile's motion are independent.

$$x = (v_0 \cos \theta_0)t, \quad v_x = v_0 \cos \theta_0,$$
$$y = (v_0 \sin \theta_0)t - \frac{1}{2}gt^2, \quad v_y = v_0 \sin \theta_0 - gt.$$

Sample Question

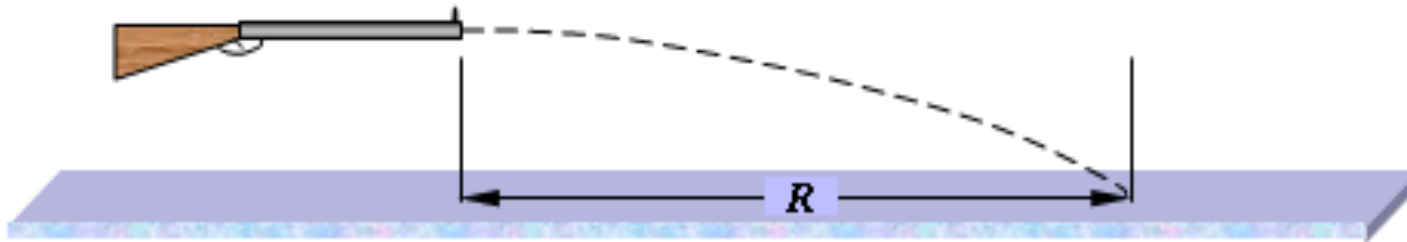
- A spring-loaded gun is aimed horizontally and is used to launch identical balls with *different initial speeds*. The gun is at a fixed position above the floor. The balls are fired one at a time. If the speed of the second ball fired is twice the speed of the first ball fired, how is the horizontal range (denoted R in the figure) affected?



- A. The range of the second ball will be twice as large as that of the first ball.
- B. The range of the second ball is about 1.4 times larger than that of the first ball.
- C. The range of the second ball will be smaller by a factor of 1.4.
- D. The range for both balls will be the same.
- E. The range of the second ball will be half as much as that of the first ball.

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$$y = y_0 + v_{y0}t + \frac{1}{2}at^2$$

$$= y_0 - \frac{1}{2}gt^2$$

$$= 0$$

$$\Rightarrow \frac{1}{2}gt^2 = y_0$$

$$\Rightarrow t = \sqrt{2y_0/g}$$

same regardless of v_x

$$\Delta x = v_{x0}t$$

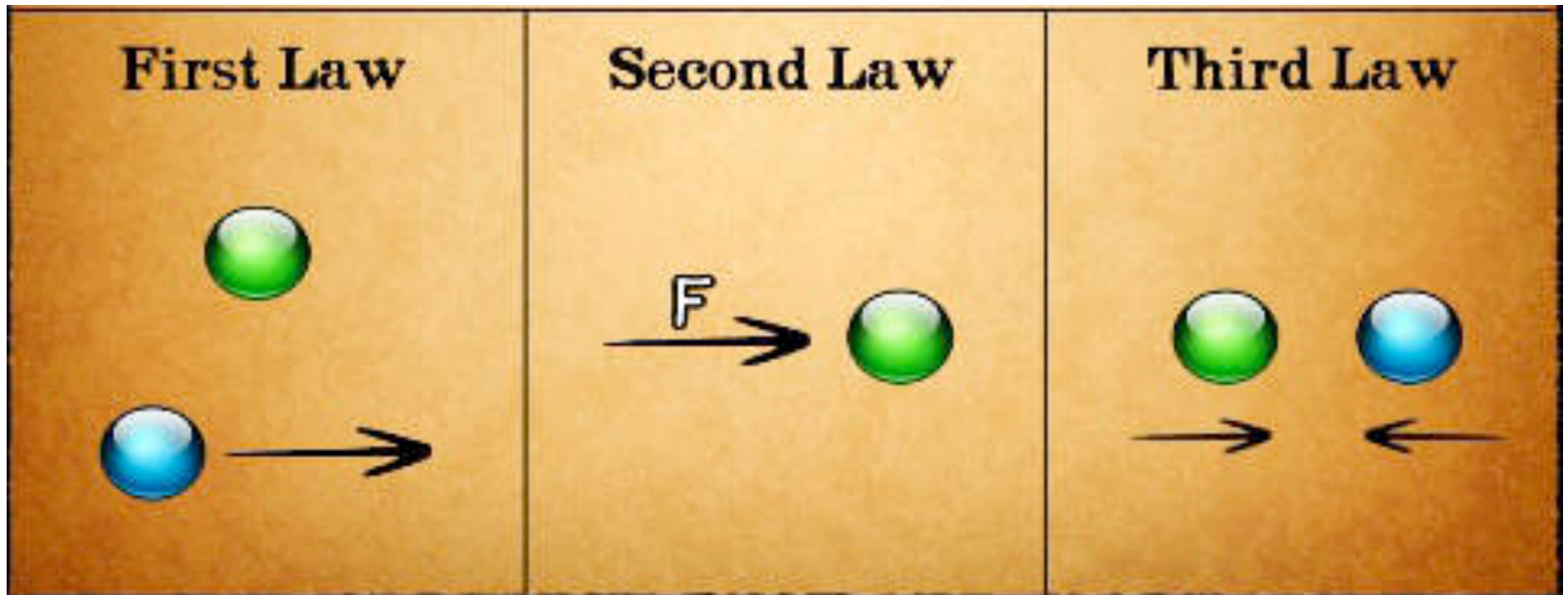
double $v_{x0} \rightarrow$ double t

Newton's Laws

Newton's Laws:

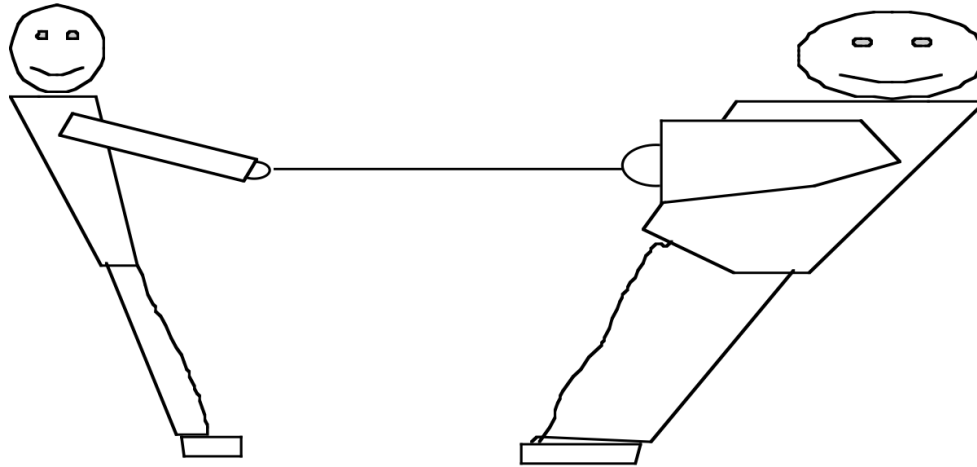
$$\sum \vec{F} = m\vec{a}$$

$$\vec{F}_{AB} = -\vec{F}_{BA}$$



Sample Question

Steve and a Sumo wrestler are having a tug-of-war. So far, no one is winning.



How does F_s (the magnitude of the force of friction on Steve's feet) compare with F_w (the force of friction on the feet of the sumo wrestler)

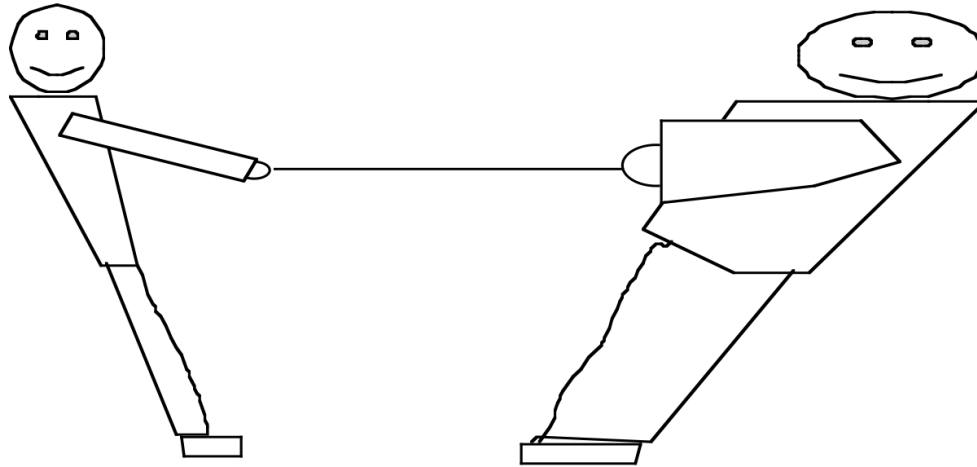
A: $F_s > F_w$

B: $F_s = F_w$

C: $F_s < F_w$.

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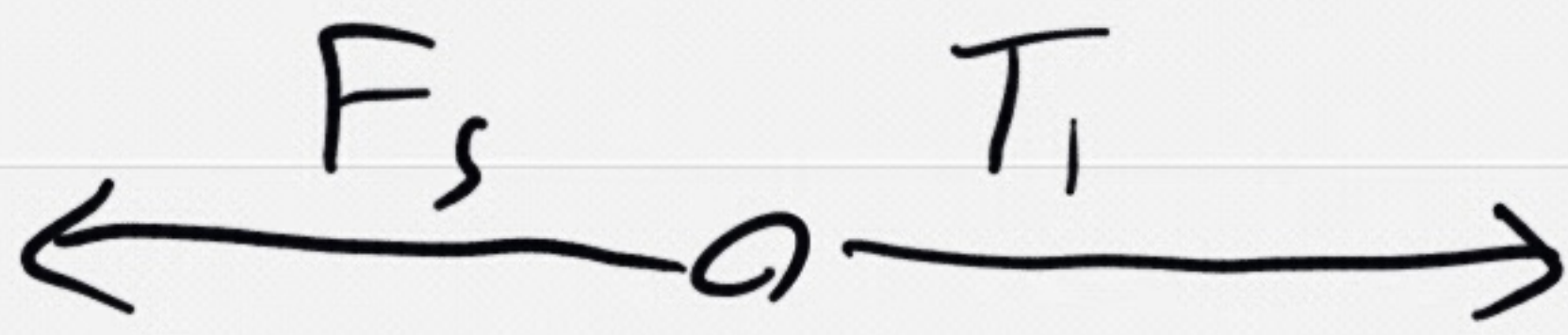
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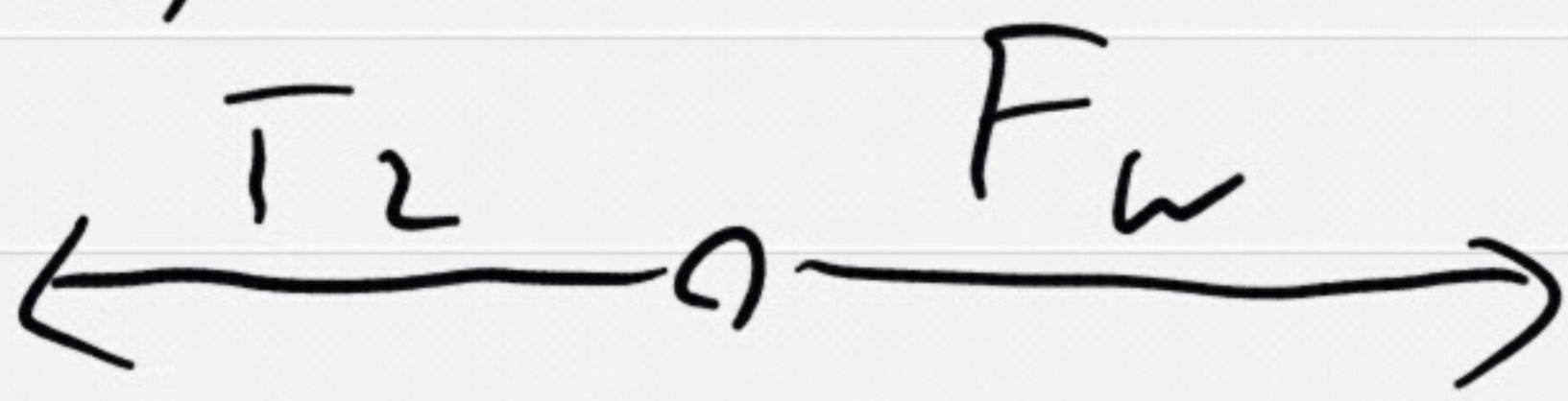
B: $F_s = F_w$

C: $F_s < F_w$.

st eve



Sumo



$$|T_1| = |T_2|$$

by Newton's 3rd

$|F_s| = |T_1|$ since not moving

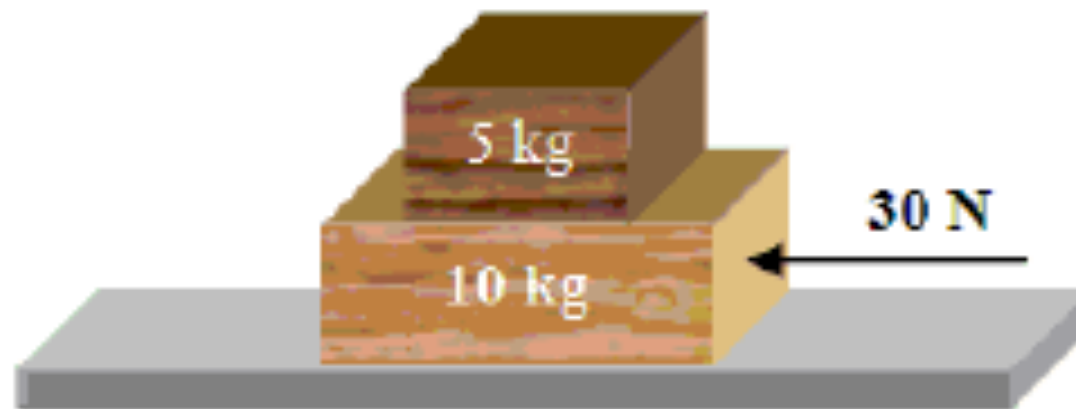
$$|F_w| = |T_2|$$

$$\Rightarrow |F_w| = |F_s|$$

Sample Question

- Two blocks rest on a horizontal *frictionless* surface as shown. The surface between the top and bottom blocks is roughened so that there is no slipping between the two blocks. A 30-N force is applied to the bottom block as suggested in the figure. What is the acceleration of the "two block" system?

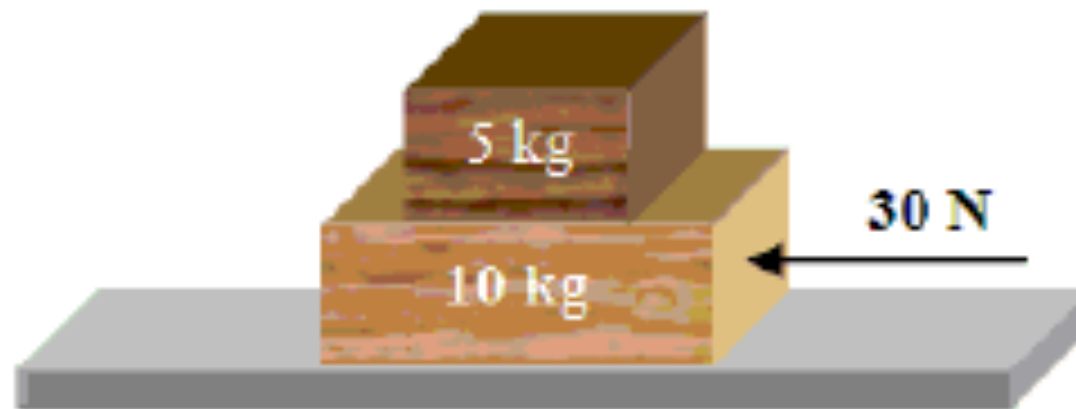
- A. 3 m/s^2
- B. 15 m/s^2
- C. 1 m/s^2
- D. 2 m/s^2
- E. 6 m/s^2



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- B. 15 m/s^2
- C. 1 m/s^2
- D. 2 m/s^2**
- E. 6 m/s^2



$$\Sigma \vec{F} = m \vec{a}$$

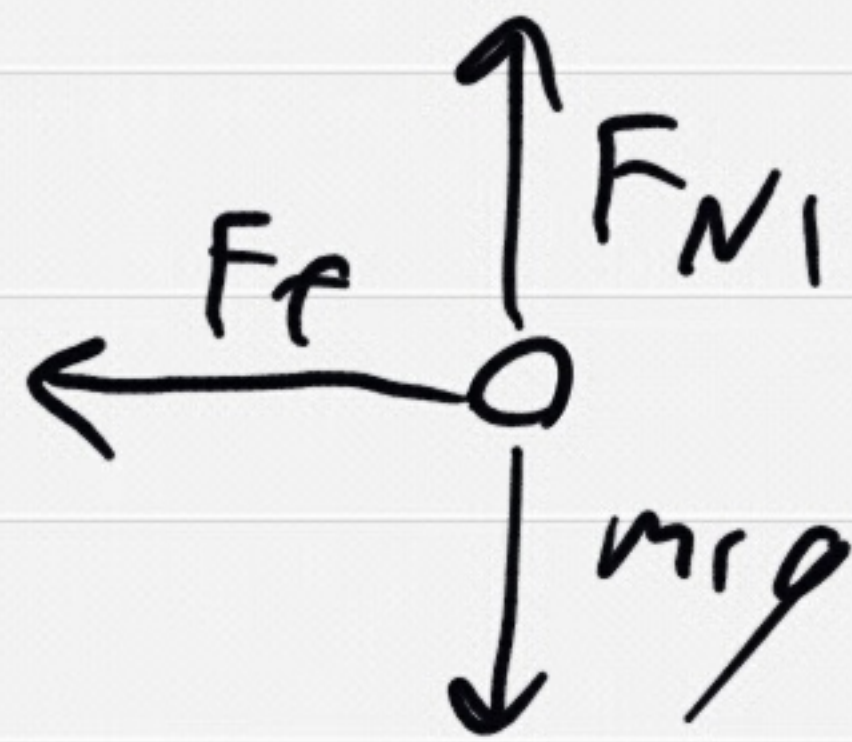
all mass accelerating together, so:

$$a = F/m$$

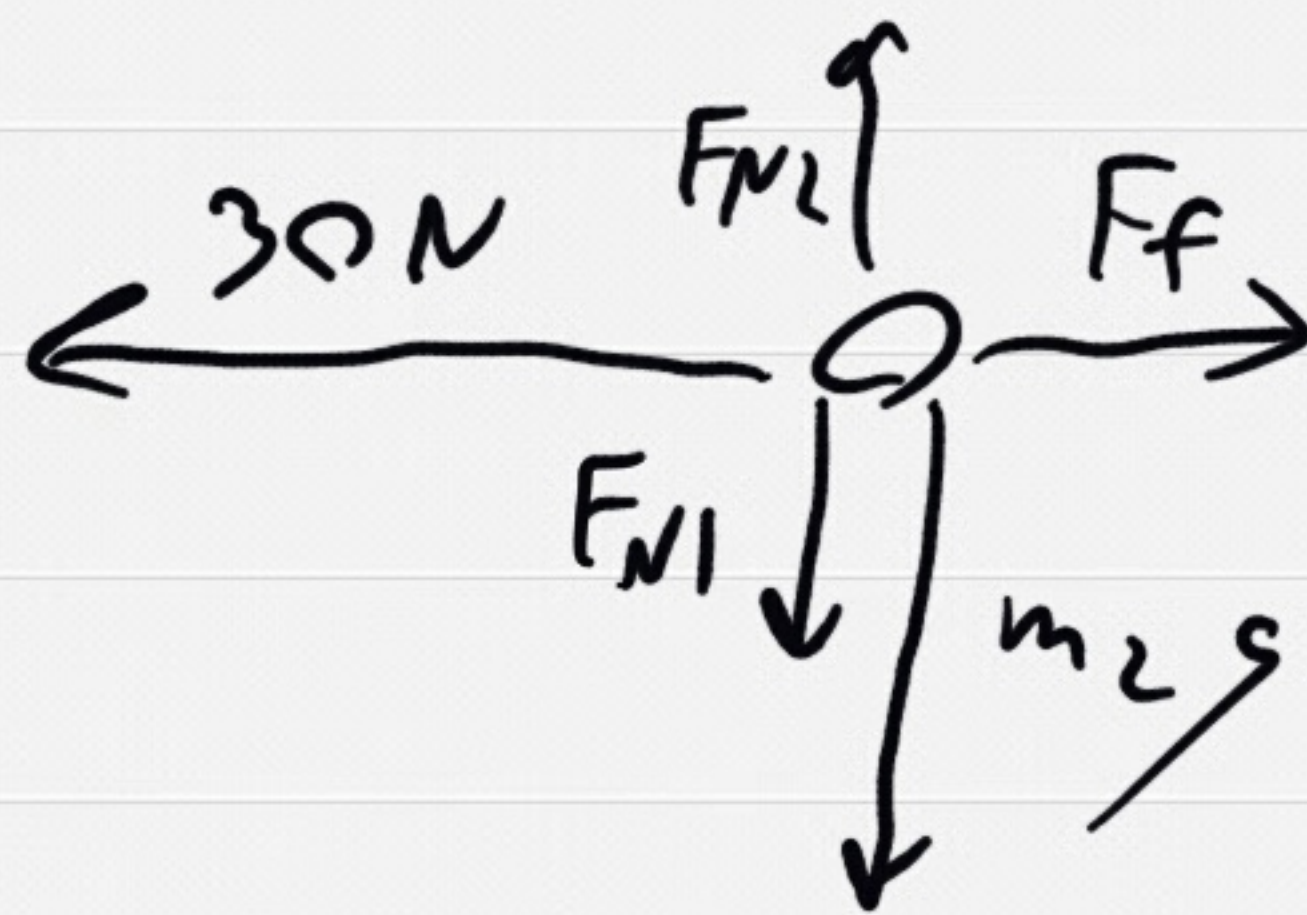
$$= 30 / (10 + 5)$$

$$= 2 \text{ m/s}^2$$

Top Block:



Bottom



$$\begin{aligned} F_f &= m_1 \cdot a \\ &= 5 \cdot 2 \\ &= \boxed{10 \text{ N}} \end{aligned}$$

$$\begin{aligned} F_{\text{net on } m_2} &= 30 \text{ N} - F_f \\ &= \boxed{20 \text{ N}} \end{aligned}$$