

$$1. a. \begin{aligned} \vec{E} &= \vec{E}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \\ \vec{B} &= \frac{\kappa}{\omega} \vec{E}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} (\hat{k} \times \hat{n}) \end{aligned}$$

$$\Rightarrow E^2 = |\vec{E}_0|^2, \quad B^2 = \frac{\kappa^2}{\omega^2} |\vec{E}_0|^2$$

$$u_D / u_E = \frac{\frac{1}{2} B^2 / \mu}{\frac{1}{2} \epsilon E^2} = \frac{1}{\mu \epsilon} \cdot \frac{\kappa^2}{\omega^2} = \boxed{1}$$

$$b. R = \langle S_R \rangle / \langle S_F \rangle = \frac{1}{2} v \epsilon E_{0R}^2 / \frac{1}{2} v \epsilon E_{0F}^2 = \frac{E_{0R}^2}{E_{0F}^2} = \boxed{(1-\beta / (1+\beta))^2}$$

$$T = \frac{1}{2} (\epsilon_0 E_{0T}^2) / \frac{1}{2} v \epsilon E_{0F}^2 = \frac{\epsilon_0}{v \epsilon} \left( \frac{2}{1+\beta} \right)^2$$

$$w/ \beta = \frac{\mu_2 n_2}{\mu_1 n_1} = \frac{\mu}{\mu_0 n} = \frac{\mu}{\mu_0} \cdot \sqrt{\frac{\mu_0 \epsilon_0}{\mu \epsilon}} = \sqrt{\frac{\mu \epsilon_0}{\mu_0 \epsilon}}$$

$$2. a. \begin{aligned} \vec{E} &= -\nabla V - \frac{\partial \vec{A}}{\partial t} \\ &= -\frac{\partial V}{\partial x} \hat{x} - \frac{\partial \vec{A}}{\partial t} \\ &= \frac{B}{(x-vt)^2} \hat{x} - \frac{Bv}{c^2(x-vt)^2} \\ &= \frac{B(1-v^2/c^2) \hat{x}}{(x-vt)^2} \end{aligned}$$

$$\vec{B} = \nabla \times \vec{A} = \mathbf{0}$$

$$2. b. \nabla \cdot \vec{A} = \frac{\partial A_x}{\partial x} = -\frac{Bv}{c^2(x-vt)^2} \neq 0$$

$$\mu_0 \epsilon_0 \frac{\partial V}{\partial t} = \frac{1}{c^2} \frac{Bv}{(x-vt)^2} \Rightarrow \boxed{\text{Lorenz}}$$

$$2.c. \quad V_{LW} = \frac{1}{4\pi\epsilon_0} \frac{qc}{(Dr - \Delta r - \vec{v})} = \frac{1}{4\pi\epsilon_0} \frac{q}{\Delta r (1 - v/c)}$$

on x-axis

$$\Delta r = x - vt_r$$

$$\text{w/ } t_r = t - \Delta r/c$$

$$\Rightarrow \Delta r = x - vt + v\Delta r/c$$

$$\Rightarrow \Delta r = (x - vt) / (1 - v/c)$$

$$\Rightarrow V_{LW} = \frac{q}{4\pi\epsilon_0} \frac{1}{x - vt} //$$

$$\vec{A}_{LW} = \frac{\vec{v}}{c^2} V_{LW} //$$

$$3.a. \quad \vec{p} = qd \cos(\omega t) \hat{z}$$

$$\ddot{\vec{p}}(t_0) = -qd\omega^2 \cos(\omega t_0) \hat{z} \quad \text{w/ } t_0 = t - r/c$$

$$\vec{S}(\vec{r}, t) \approx \frac{\mu_0 \dot{p}^2}{16\pi^2 c} \frac{\sin^2\theta}{r^2} \hat{r}$$

$$= \frac{\mu_0 q^2 d^2 \omega^4 \cos^2(\omega t_0)}{16\pi^2 c} \frac{\sin^2\theta}{r^2} \hat{r}$$

$$3.b. \quad a = \ddot{z} = -d\omega^2 \cos^2(\omega t)$$

$$\text{for } v \ll c \quad \vec{S}_{\text{rad}}(\vec{r}, t) = \frac{\mu_0 q^2 a^2}{16\pi^2 c} \frac{\sin^2\theta}{\Delta r^2} \Delta \vec{r}$$

$$\text{for } d \ll r, \quad \Delta \vec{r} \sim \vec{r}$$

$$\Rightarrow \vec{S}_{\text{rad}} \sim \frac{\mu_0 q^2 d^2 \omega^4 \cos^2(\omega t_r)}{16\pi^2 c} \frac{\sin^2\theta}{r^2} \hat{r}$$

$$\text{w/ } t_r = t - r/c$$