

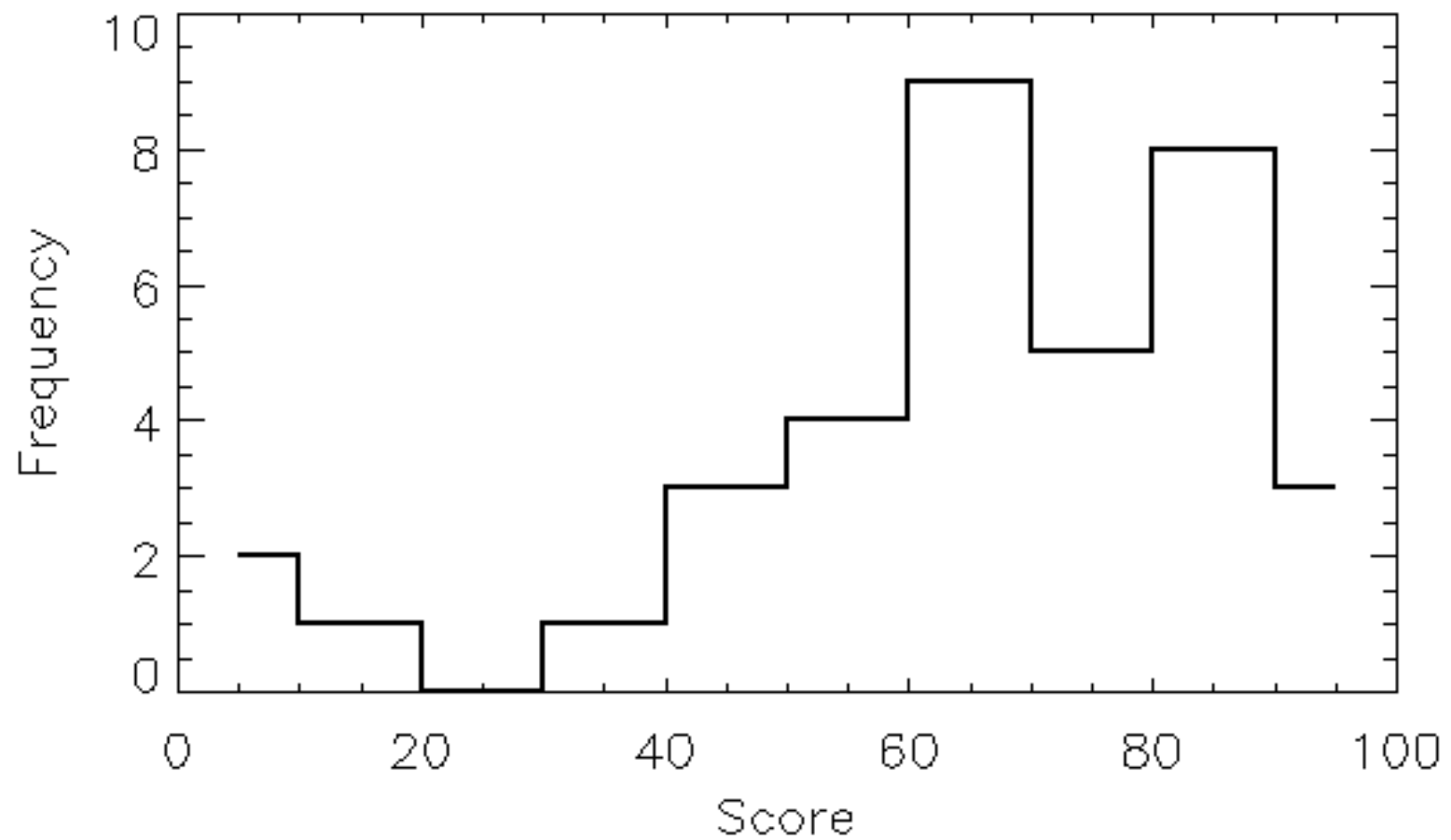
Modern Physics (Phys. IV): 2704

Professor Jasper Halekas
Van Allen 70
MWF 12:30-1:20 Lecture

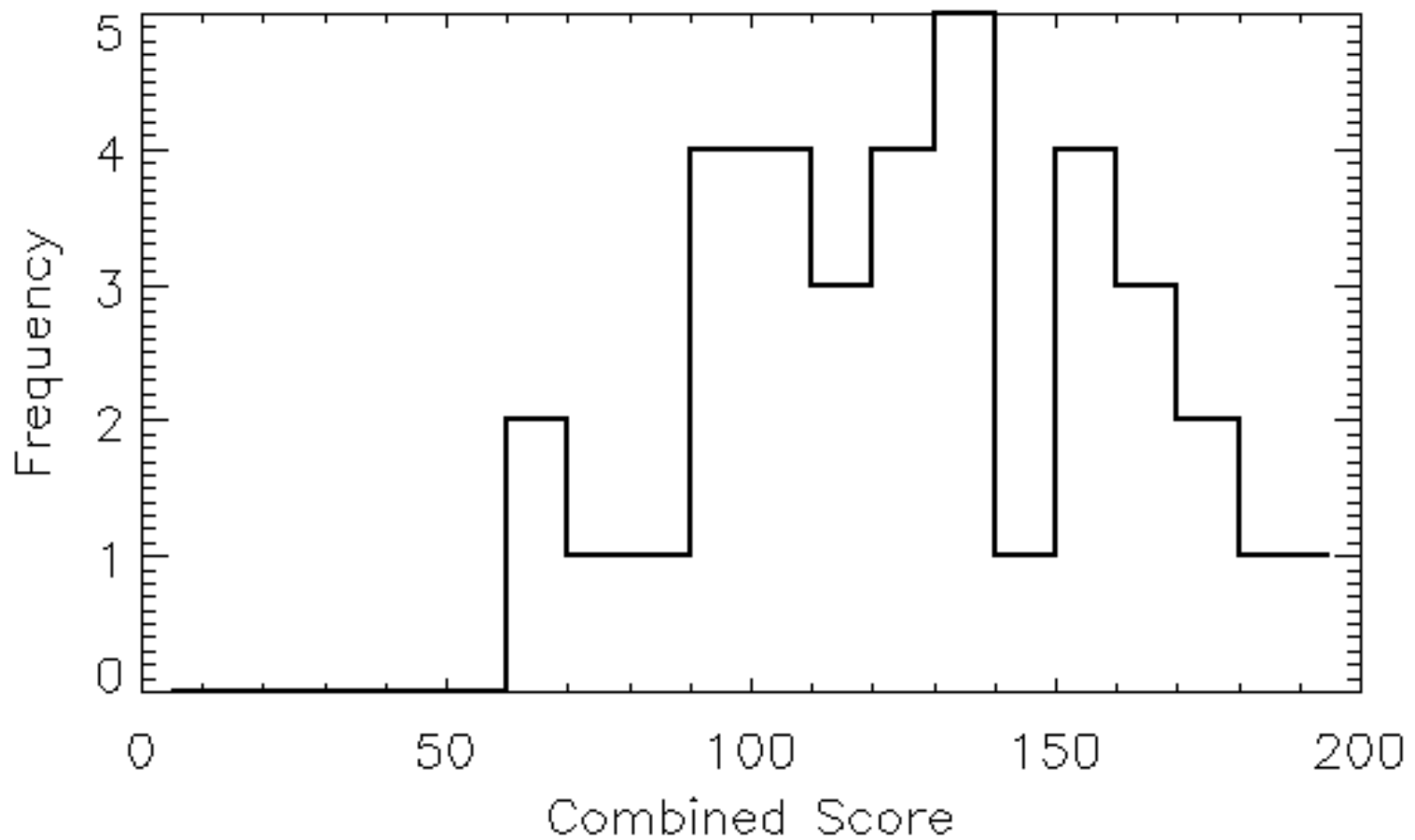
Midterm II Is a Wrap

- Mean of 34 people who took the test
 - 69/100
- Mean of entire class including 2 absentees
 - 65/100

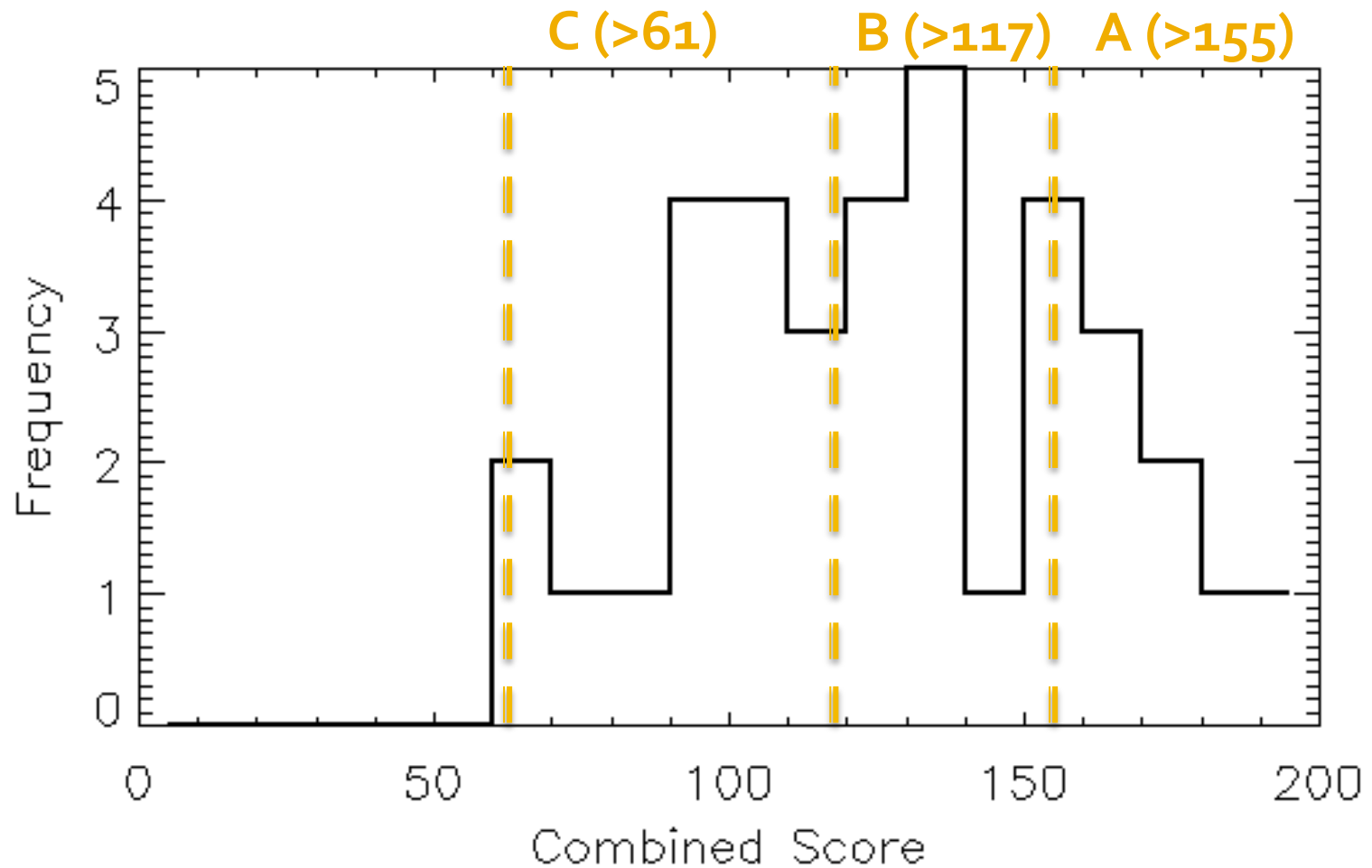
Midterm II Scores



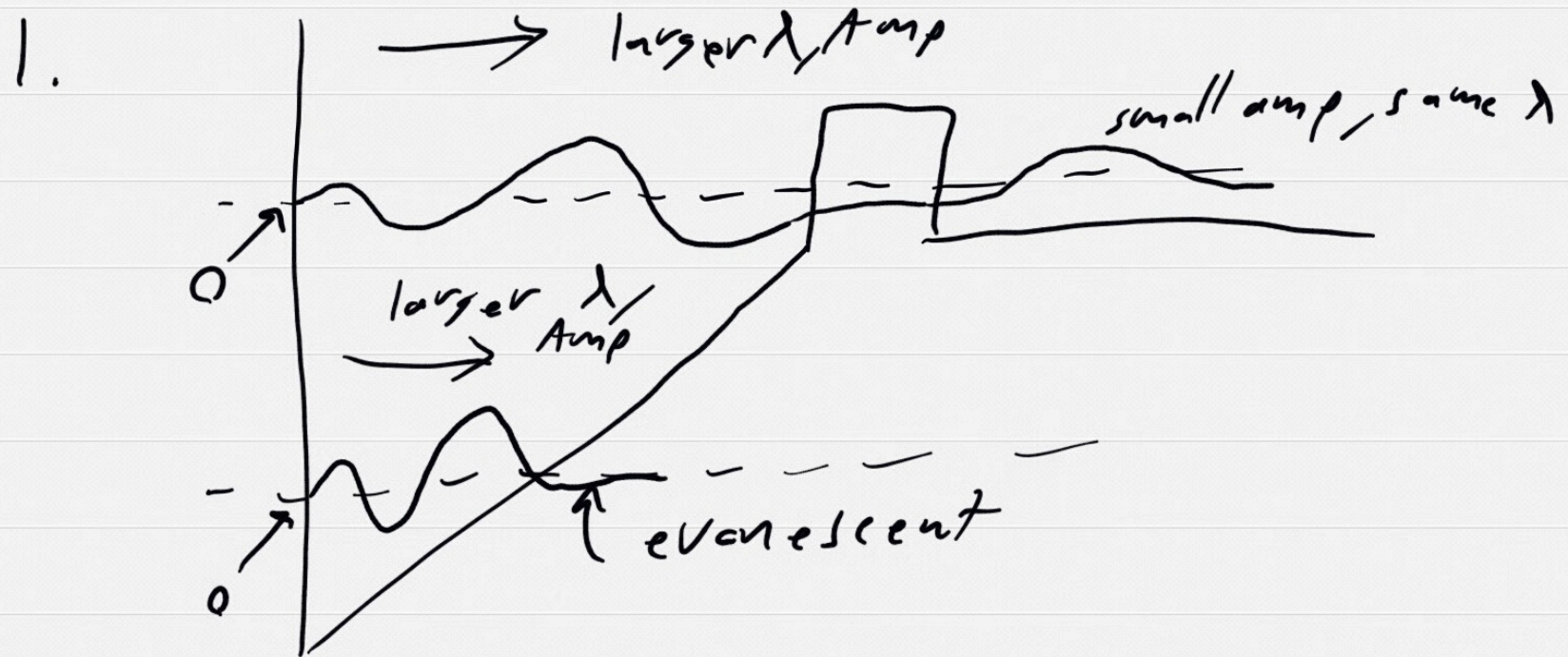
Combined Exam Scores



Very Approximate Grade Equivalents from CLAS Curve (Does Not Include Labs, HW, or Participation Extra Credit!!!)



Q1 Key Points



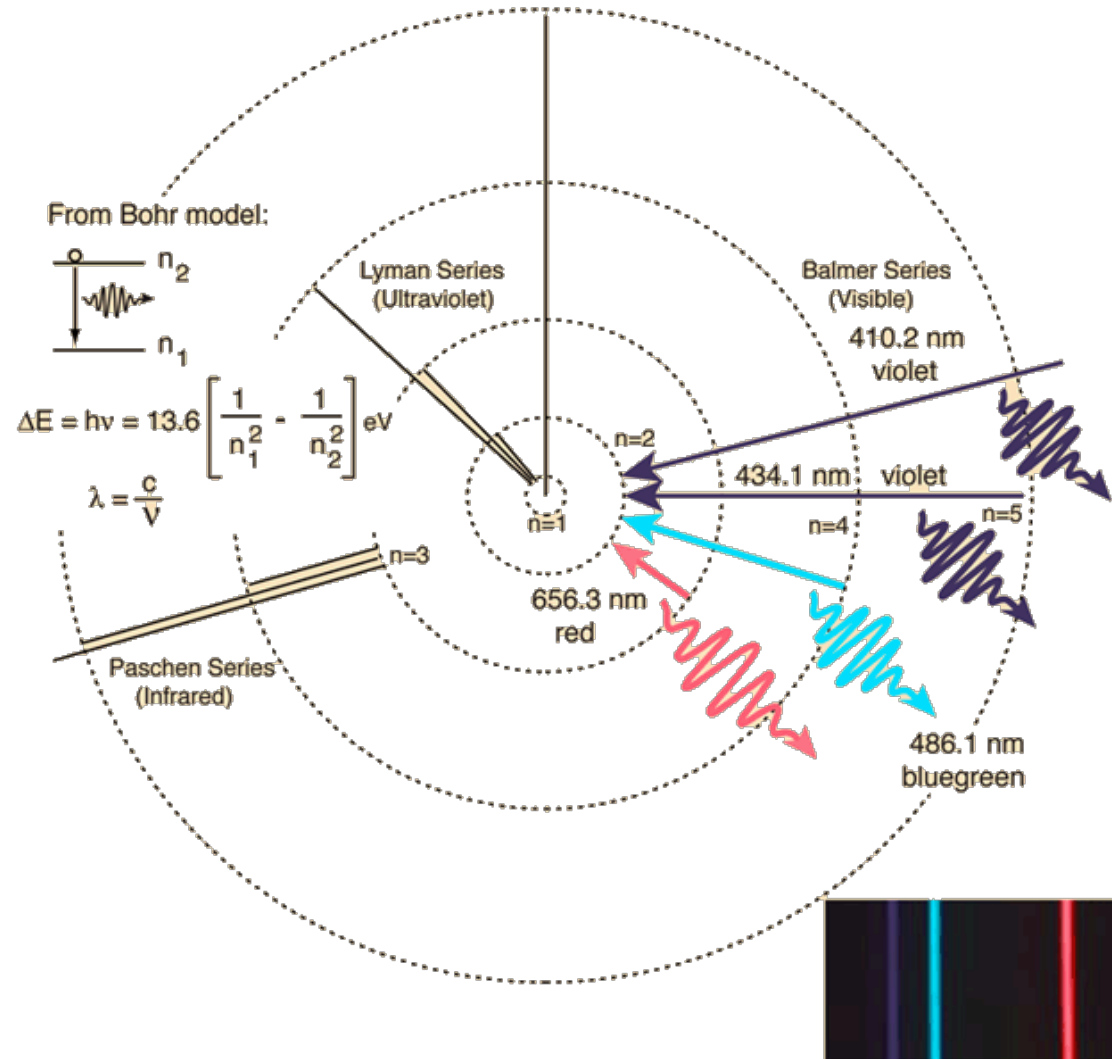
Q2 Key Points

$$\frac{-\hbar^2}{2m} \frac{d^2\Psi(x)}{dx^2} + U(x)\Psi(x) = E\Psi(x)$$

- Schrödinger equation must be satisfied for **all** values of x
 - All terms that don't depend on x must cancel, and all terms with a given power of x must cancel

Q3 Key Points

- Bohr energies proportional to Z^2/n^2
- Photon energies proportional to the **difference** in Bohr energies
- Longest wavelength \leftrightarrow smallest energy change



Q4 Key Points



n = principal

distance
from nucleus

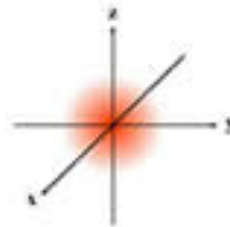
Energy



l = angular

shape
of orbital

Orbital
Angular
Momentum



m = magnetic

orientation
in space

Direction of
Orbital
Angular
Momentum

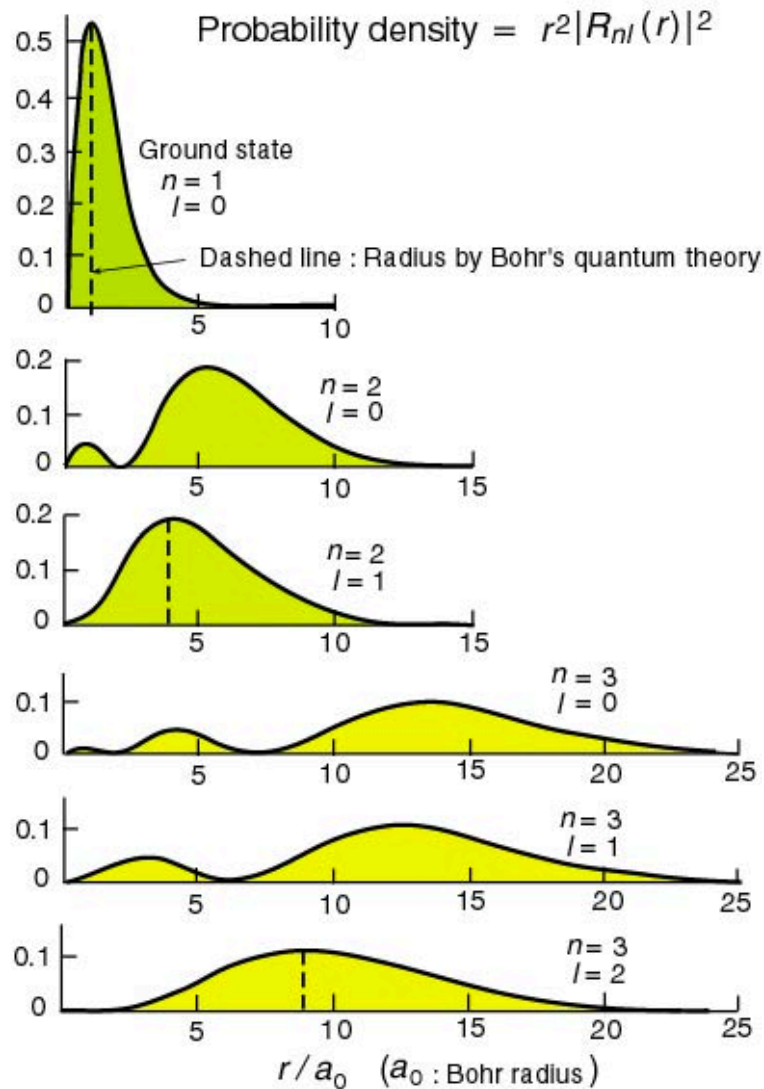


S = spin

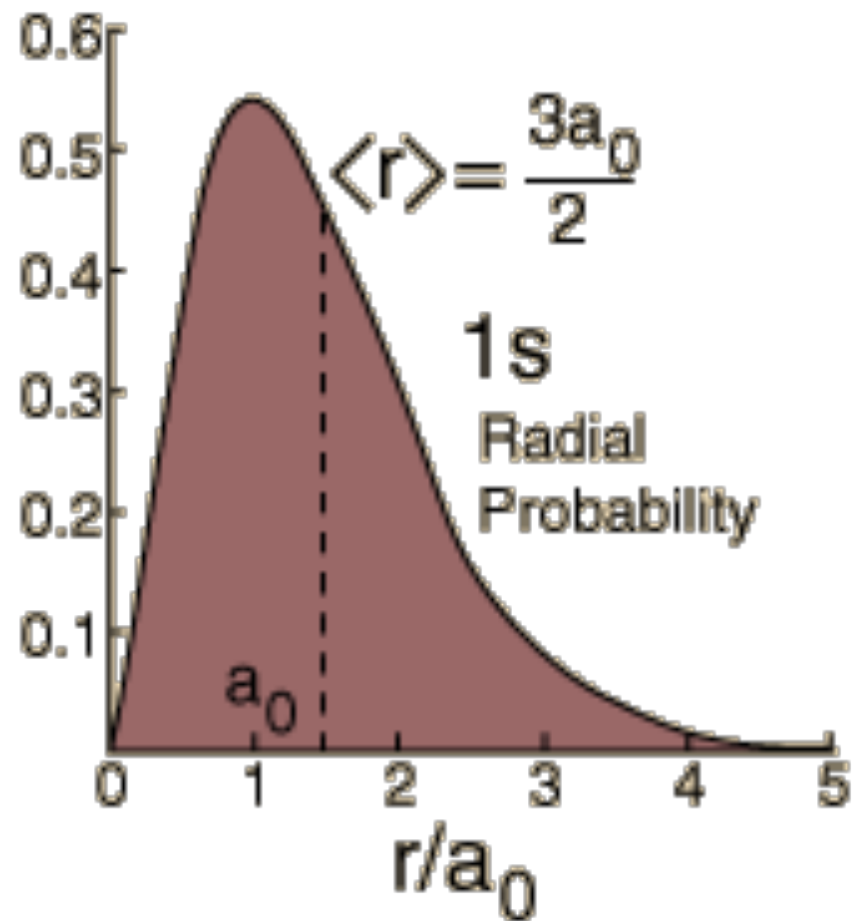
electron
spin

Rotational
Angular
Momentum

Q5 Key Points



$$\langle r \rangle = \int_0^{\infty} rP(r)dr$$



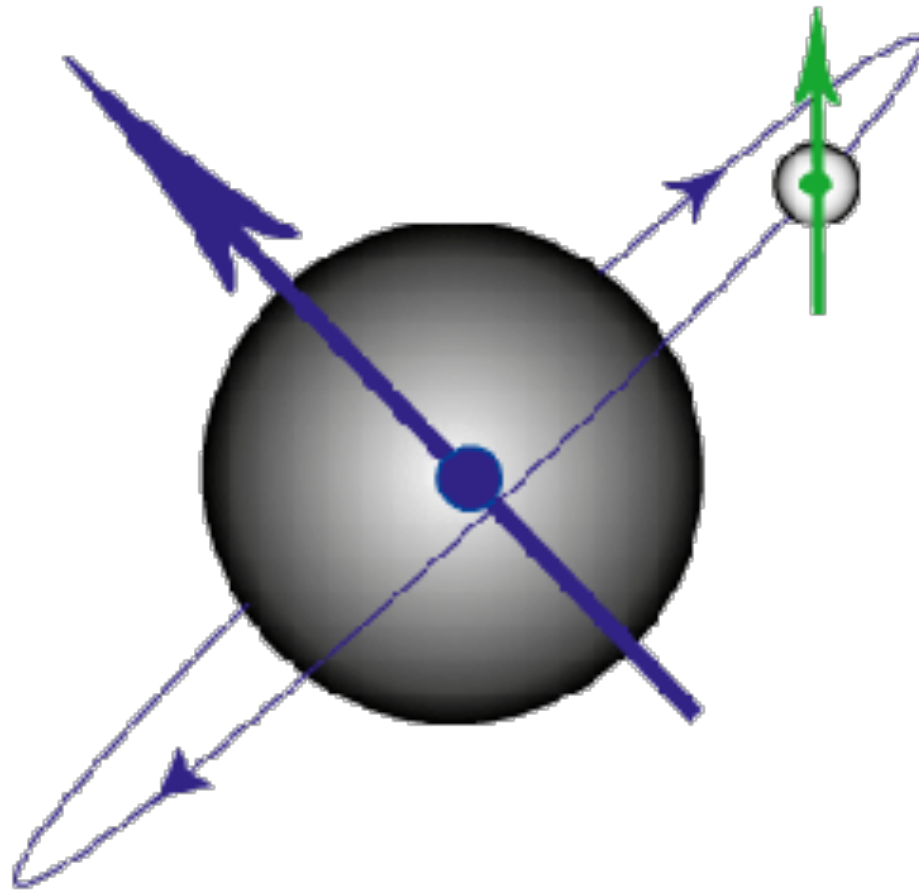
Q6 Key Points



$$|Y_{2,1}^{1/2}(\theta, \phi)|^2$$

- All angular probability densities are constant with azimuthal angle since $|e^{im\phi}| = 1$
- Direction of angular momentum is not the same as location of maximum probability!

Orbital and Spin Magnetic Moment



Orbital and Spin Magnetic Moment

$$\mu_B = \frac{e\hbar}{2m_e} = 9.2740154 \times 10^{-24} \text{ J / T} = 5.7883826 \times 10^{-5} \text{ eV / T}$$

Bohr magneton

Orbital $\mu_L = -g_L \frac{e}{2m_e} L$ $\mu_{Lz} = -g_L \frac{e\hbar}{2m_e} m_\ell = -m_\ell \mu_B$

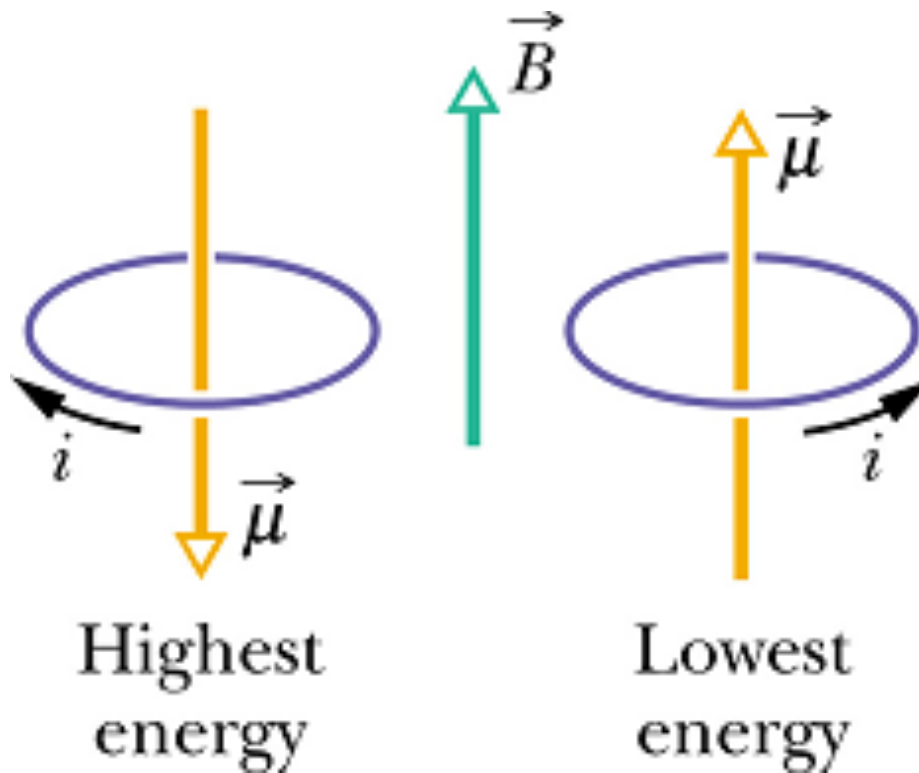
since $g_L = 1$

Spin $\mu_S = -g_S \frac{e}{2m_e} S$ $\mu_{Sz} = -g_S \frac{e\hbar}{2m_e} m_s = -2m_s \mu_B = \pm \mu_B$

$g_S = 2.0023 \approx 2$

Magnetic Moment in Magnetic Field

$$U_{mag} = -\vec{\mu} \cdot \vec{B}$$



Concept Check

- An electron is in the $n = 2, l = 1$ orbital. An external magnetic field is in the +Z direction. For which m_l is the electron energy lowest?
 - A. -1
 - B. 0
 - C. 1
 - D. All same

Concept Check

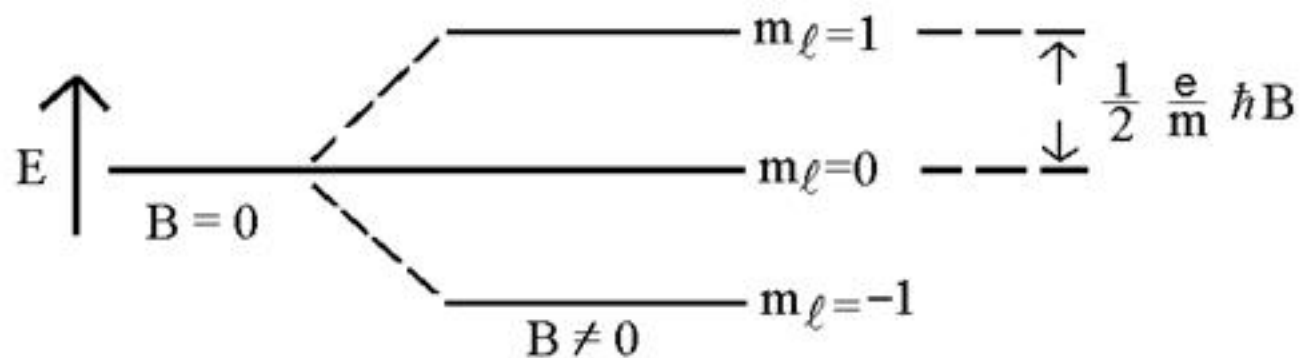
- An electron is in the $n = 2, l = 1$ orbital. An external magnetic field is in the +Z direction. For which m_l is the electron energy lowest?

A. -1

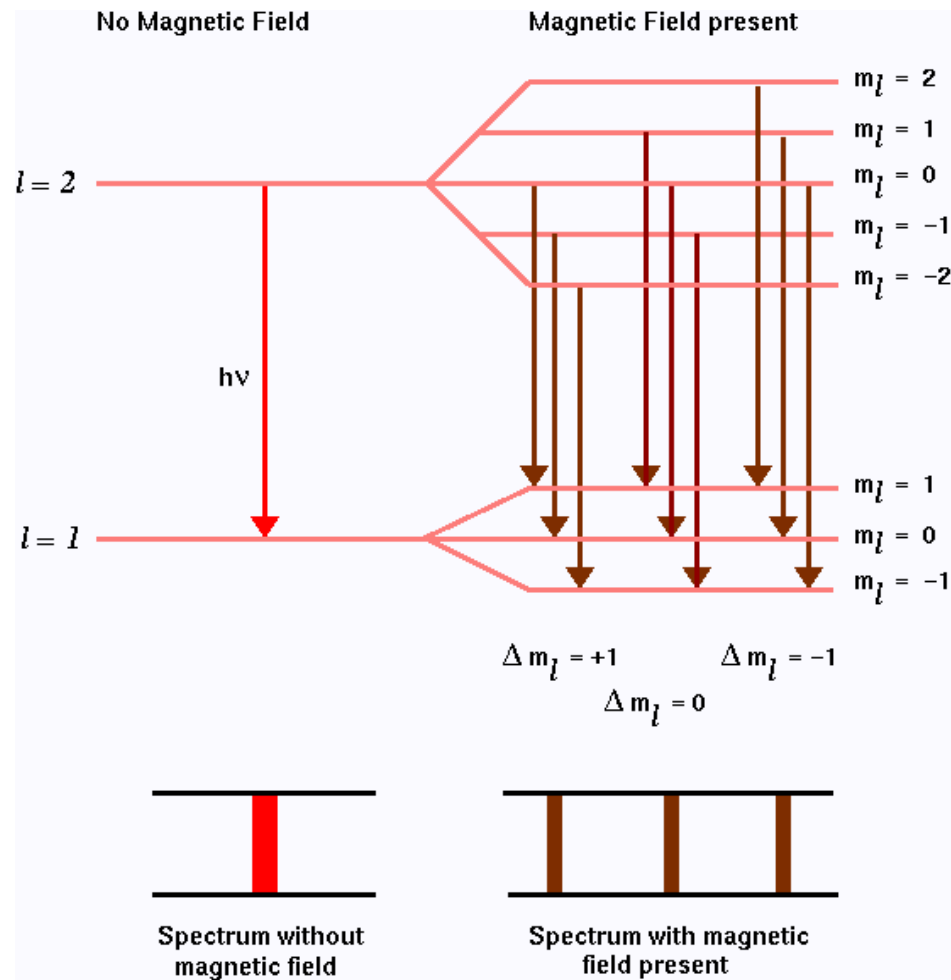
B. 0

C. 1

D. All same

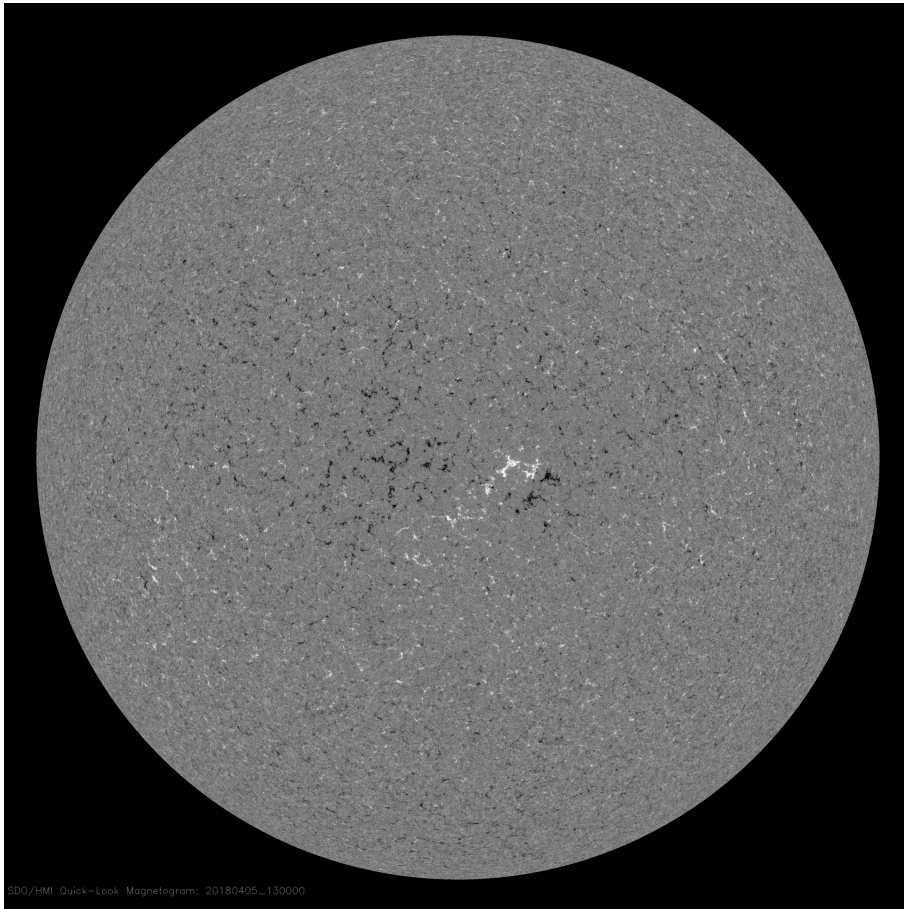


Zeeman Effect

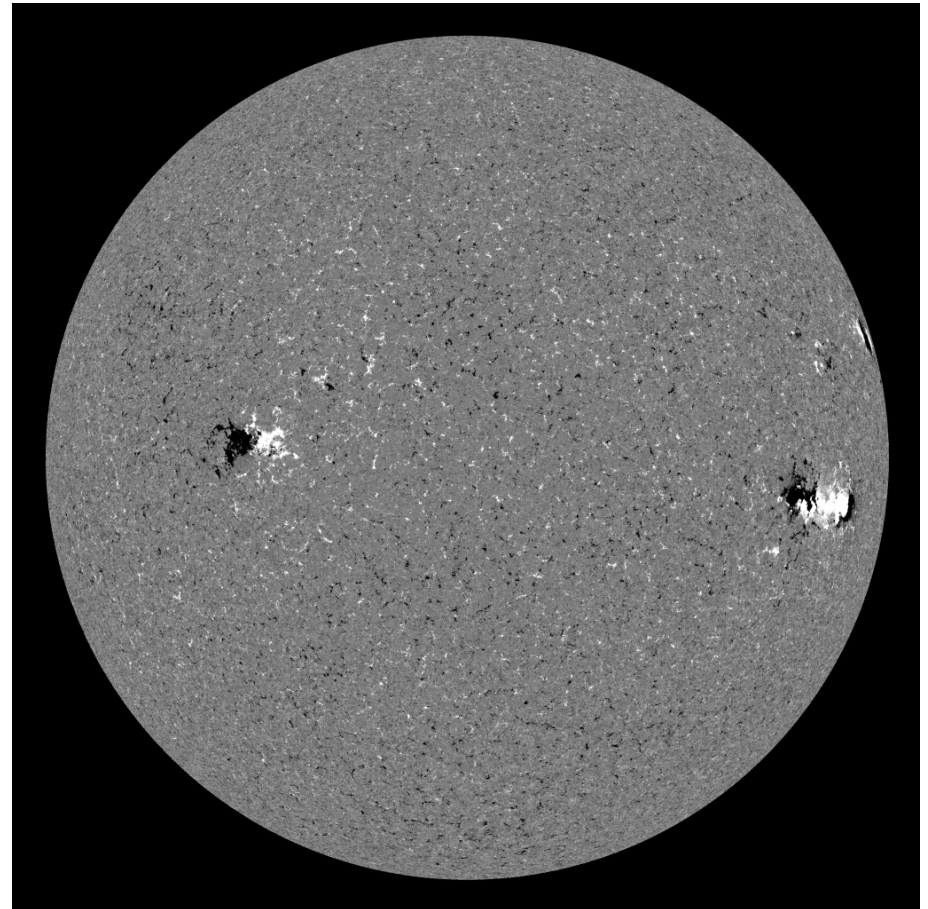


Magnetogram

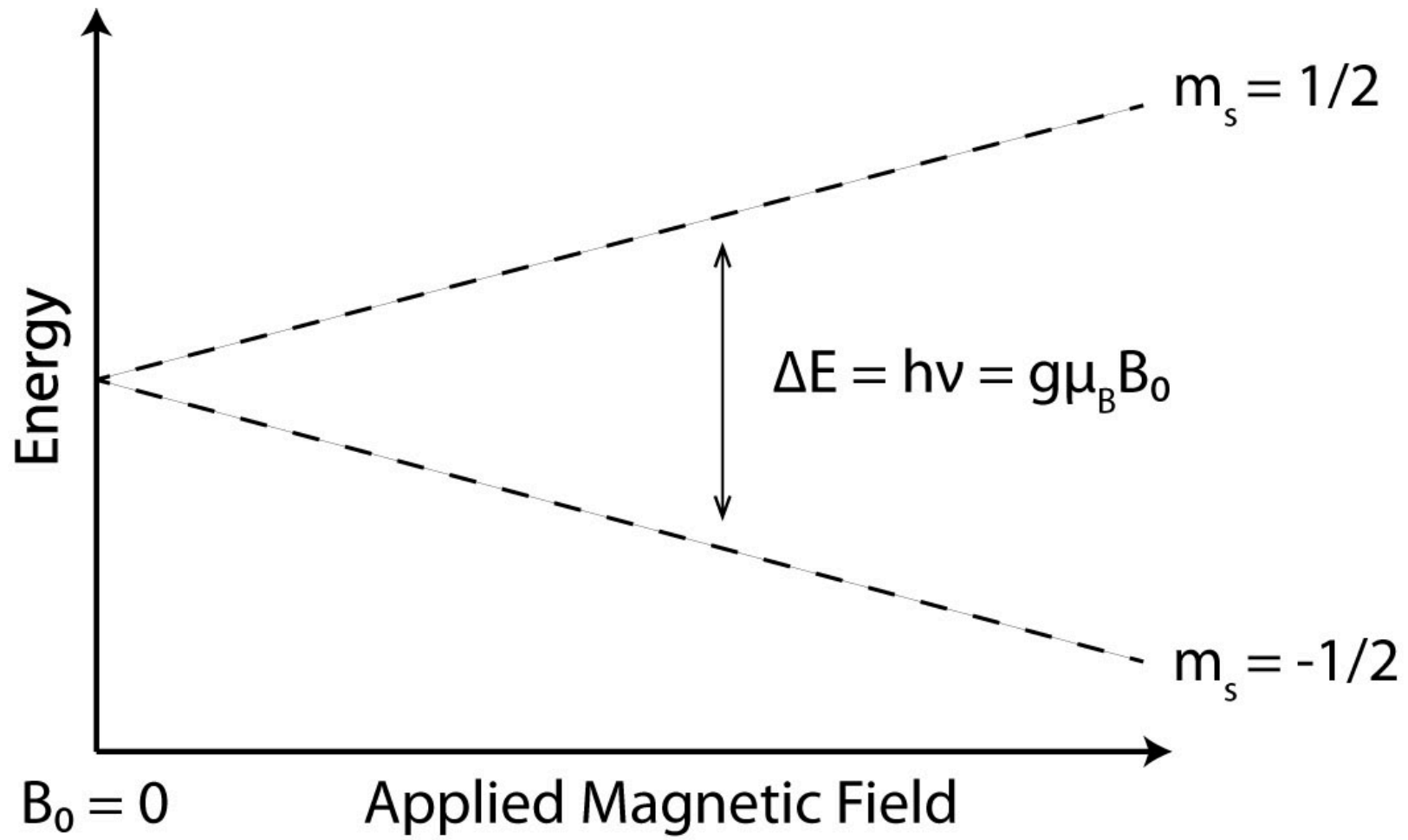
2018/04/05 13:00:00



2017/04/05 12:10:38

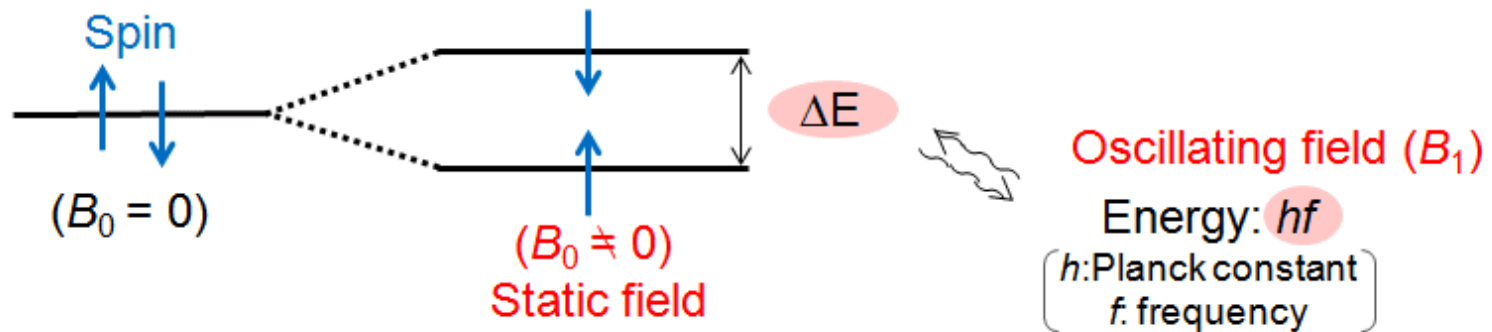


"Anomalous" Zeeman Effect



Electron Spin Resonance

Principle of ESR



Up-spin and down-spin have same energy

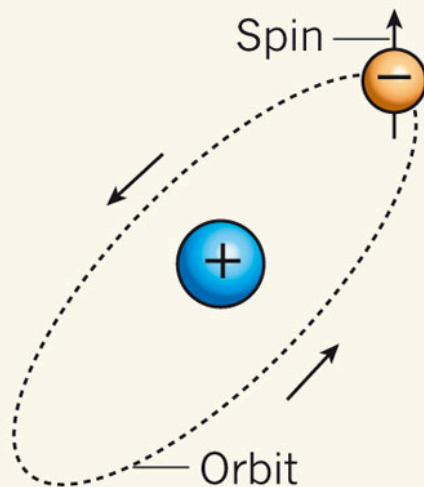
Static field (B_0) induces energy splitting (ΔE) between up-spin and down-spin

Resonance occurs when hf matches ΔE matches

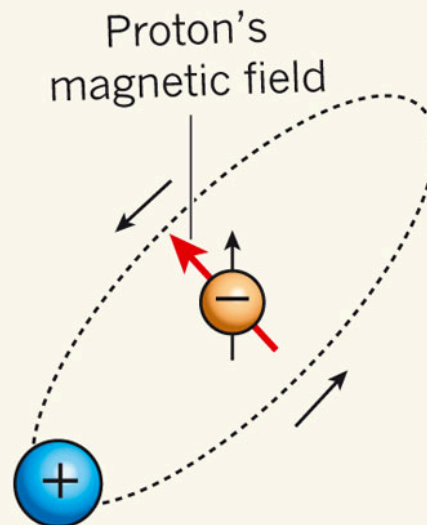
Spin-Orbit Coupling

a Electron in an atom

Proton's point of view



Electron's point of view

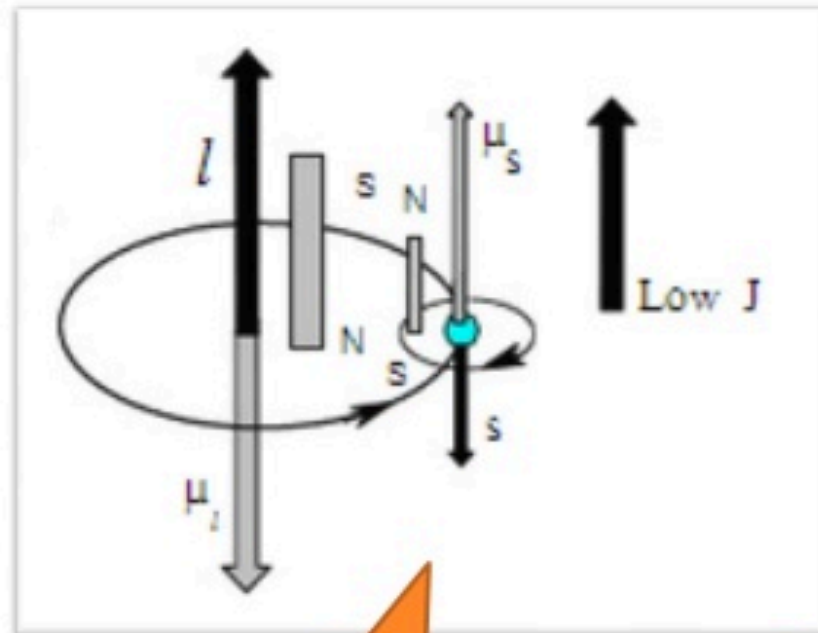
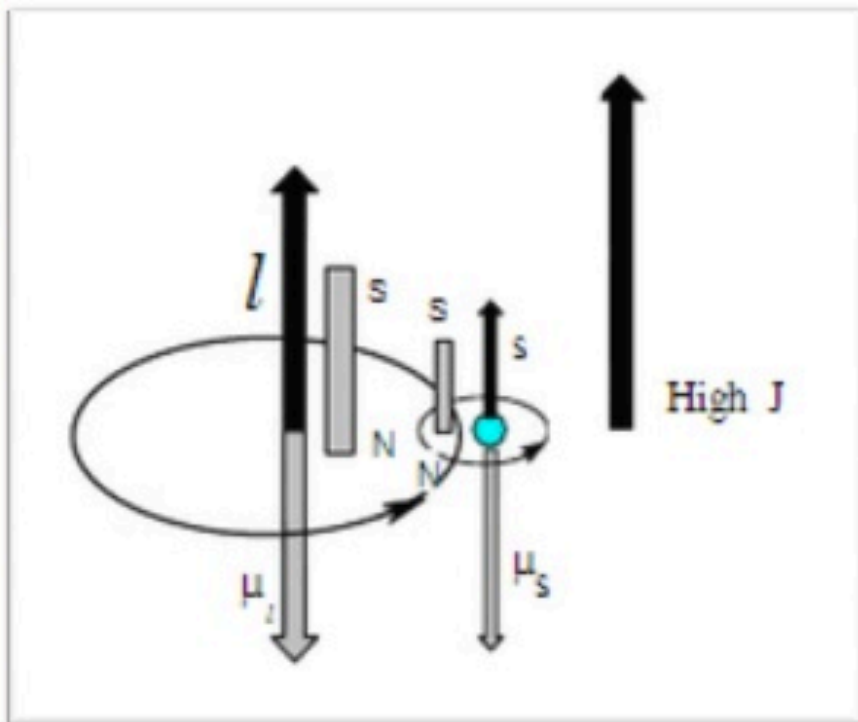


Electron orbit around proton causes field B in electron frame.

This leads to a shift in energy due to interaction of the electron spin magnetic moment with B .

Spin moment aligned (spin anti-aligned) with B has lower energy.

Spin-Orbit Coupling



Lower energy !

Spin-Orbit Level Splitting

