

1. Total  $E$  conserved  
Initial  $KE = 0$ , final  $KE > 0$   
some rest energy was converted  
to  $KE$ . So  $2m < M$

2. a.  $L' = L_0 = 10 \text{ m}$   
 $L = L' / \gamma = 6 \text{ m}$   
 $ct = cL / v = 7.5 \text{ m}$

so  $x_2 = 0, ct_2 = 7.5$

b.  $x_2' = -10, ct_2' = 12.5$

c.  $\Delta s^2 = 7.5^2 = 56.25$   
 $\Delta s'^2 = 12.5^2 - 10^2 = 56.25$   
 $\Delta s'^2 = \Delta s^2$  (always true)

3.  $E_i = 2E\gamma$   
 $p_{xi} = \frac{E\gamma}{c} \cos(60^\circ) + \frac{E\gamma}{c} \cos(60^\circ)$   
 $= \frac{E\gamma}{c}$   
 $p_{yi} = 0$

$E_f = 2E\gamma, p_f = [E\gamma/c, 0]$

$Mc^2 = \sqrt{(2E\gamma)^2 - (p_f c)^2} = \sqrt{3E\gamma^2}$

$\Rightarrow M = \sqrt{3} E\gamma / c^2$



4. Faster electrons  
 $\Rightarrow$  more momentum  
 $\Rightarrow$  smaller wavelength  
 $\Rightarrow$  decreased spacing

5. a.  $\Delta \nu = \Delta E / h$   
 $=$   $250,000 \text{ e} / h$

b.  $\Delta \lambda = .0024 \text{ nm} (1 - \cos \theta)$   
 $\lambda_i = 0.0024 \text{ nm}$   
 $\Rightarrow E_i = hc / \lambda_i = 1200 / 0.0024$   
 $= 500,000 \text{ eV}$

$E_f = 250,000 \text{ eV}$

$\Rightarrow \lambda_f = .0048 \text{ nm}$

$\Delta \lambda = 0.0024 \text{ nm} \Rightarrow \cos \theta = 0$

$\Rightarrow$   $\theta = 90^\circ$

6.  $\Delta E \Delta t \sim \hbar \sim 10^{-15} \text{ eV s}$

$\Delta t \sim 10^{-15} / (2.500000)$

$=$   $10^{-21} \text{ s}$

